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Analysis of Transients in Wind Parks: Modeling of System Components and Experimental Verification

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Abey Daniel & Samson Gebre

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Department of Electric Power Engineering
Division of Energy and Environment
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Analysis of Transients in Wind Parks: Modeling of System Components and Experimental Verification

Abey Daniel & Samson Gebre

Performed at: ABB Corporate Research
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Advisor: Ambra Sannino
ABB Corporate Research
Västerås, Sweden

Examiner: Torbjörn Thiringer
Division of Electric Power Engineering
Department of Energy & Environment
Chalmers University of Technology

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ABEY DANIEL & SAMSON GEBRE

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Department of Energy and Environment
Chalmers University of Technology
SE-412 96 Göteborg
Sweden
Telephone + 46 (0)31-772 1000
E-mail: abiy1882@yahoo.com
gebrsa@yahoo.com

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ABSTRACT

This thesis deals with analysis of transients and experimental verifications in wind parks. The focus is on accurate modeling of system components such as cables, vacuum circuit breakers and transformers which make any branch in a wind park. Models are also validated where possible. Although a lot has been done and fairly good models of cables and VCBs have been developed, it seems that a unified wide band model of transformers which works well for broad range of frequencies has been the most difficult to develop. Critical as it is in transient studies, modeling of such a transformer has been extensively treated in this thesis.

In the first part of the thesis, a frequency dependent model which represents high frequency effects like wave propagation, damping and reflection is used to model the cables using PSCAD/EMTDC. The model is also validated experimentally. Secondly, a statistical model which emulates the occurrence of re-ignitions, pre-strikes and current chopping behaviors of the VCB during opening or closing operations is dealt with. Finally, a terminal model of a transformer which represents its wide frequency response is developed based on experimental measurement of admittance matrix over a wide range of frequencies. The curve fitting algorithm is used to approximate the admittance matrix. An RLC equivalent network is realized and implemented in the time simulation software PSCAD/EMTDC.

PREFACE

This thesis work was conducted at ABB corporate research. We would like to express our deepest gratitude to our supervisor Ambra Sannino for providing us with the opportunity to work in an excellent academic environment and for her brilliant ideas, guidance and inspiration.

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ABBREVIATIONS

VCB	Vacuum Circuit Breaker
BIL	Basic Insulation Level
MV	Medium Voltage
WP	Wind Park
EMTP	Electro Magnetic Transient Program
PSCAD	Power System CAD
EMTDC	Electromagnetic Transient with DC
TOV	Transient Overvoltage
EM	Electromagnetic
RRDS	Rate of Rise of Dielectric Strength

Chapter 1

INTRODUCTION

1.1 Problem description

Nowadays due to the development of modern circuit breakers; vacuum and SF6 for example, the switching overvoltage has become a more severe problem, to some extent caused by the fact that the current interruption capabilities of these breakers have improved significantly [3]. These switching transient over voltages have the potential to result in large financial losses. Transient overvoltages and other power quality disturbances cause billions of dollars of losses each year due to damage to equipment and loss of production [1]. Worldwide many transformer insulation failures have been reported caused by switching transients [5], [6], while those transformers had previously passed all the standard tests and complied to all quality requirements. These phenomena can occur in both distribution and transmission networks. The problem is generally associated with the fast transient over voltages produced by re-strikes and pre-strikes during the opening or closing of a switching device. Especially the vacuum circuit breaker (VCB), which shows a high ability of interrupting high frequency currents of several hundreds of kHz, may cause switching overvoltages with fast rise time and thus degrading the insulation and eventual failure due to the cumulative effect of voltage transients of even less magnitude than the BIL.

The use of a cable network and VCB in medium voltage (MV) networks could be a source of insulation failure due to the fast voltage transients caused by multiple re-strikes of VCB. There is a similarity between wind parks (WP) and industrial MV networks in this regard as both use VCB as switching device and consists of a cable network. Hence there is a concern of transient overvoltages (TOV) in wind parks as well. One example could be Denmark's Horn Rev, one of the world's biggest off shore wind farms built to date, where all transformers and generators had to be moved to shore for maintenance. Fast switching, high voltage transients are suspected to have contributed to the failure [7].

Due to the unpredictable threat of TOV in WPs and large MV systems it is worth studying fast switching TOV in wind parks and MV systems experienced due to the unavoidable switching action of VCB. To analyze these phenomena, an experimental set-up was designed in ABB Corporate Research with three-phase cable representing a part of a wind park, including one feeder with one turbine under test and the adjacent tower and adjacent feeder to reproduce a unique wind farm in a lab. The experimental set up is also useful to study large cable systems such as MV undergrounding and industrial systems.

1.2 Overview of earlier work

A number of investigations have been done related to this work. It is not the intention of this section to summarize these valuable works, but the interest in this section lies on overview of the two works by Daniel Mireanu and Maialen Boyra as this work is the continuation of these two. The first work provides an analysis of TOVs and their propagation in cable systems [31]. This investigation is performed through the use of two systems: an industrial steel mill electrical system and a wind farm. Cables and vacuum circuit breakers, two essential components in any MV cable system, are discussed in detail and modeled in PSCAD/EMTDC. The two systems are then simulated and, where available, the results are compared to measured data for verification. In the second work, TOVs in cable systems are characterized through both simulations in PSCAD/EMTDC and laboratory experiments which characterize a section of wind power plant [30]. A single phase laboratory set up was used which includes two single phase cables, a VCB in between, and supply side and load side transformers. The laboratory system was modeled. Analysis of measurement and simulation results were also made for different loading conditions.

1.3 Aim of this thesis

The aim of this work is to study and characterize high frequency transients in wind parks. A crucial part is accurate modeling of the cable, vacuum circuit breaker and transformer which comprise a branch in any wind park. As the work is a continuation of [30] and [31], a particular interest is to refine and improve models of the aforementioned components. Particularly, a different approach is used to model the transformer than those used in [30] and [31], one that enables representing the transformer by using a single and unified terminal model for a very wide band of frequencies.

1.4 Thesis outline

Chapter 1 gives a general background of the thesis. An overview of previous literature by is presented, [30] and [31]. The aim of this thesis work is defined as well.

Chapter 2 presents an overview of TOVs, how they are classified, their causes and how they propagate through the system.

Chapter 3 presents modelling of a power cable which is to be used later in the simulation of the whole system. The model derived in this chapter proposes a method to account for the effects of stranding of the conductor and semi conducting layers for use in PSCAD/EMTDC. Comparison of results obtained between the model and measurement data during cable discharging is also included.

Chapter 4 Describes the VCB model treated in this paper. The model simulates most of the effects (phenomena) of a VCB. Results obtained from model testing are also included in this chapter.

Chapter 5 and 6 propose the modelling of a transformer by measuring the admittance matrix in a wide frequency domain. The admittance matrix experimentally determined is subjected to a rational function approximation by vector fitting. A transformer model compatible with electromagnetic transient programs (EMTP) can then be obtained by network realization of the rational function.

Chapter 7 gives conclusions of the thesis work and suggests future work.

Chapter 2

TRANSIENT OVERVOLTAGES

2.1 Introduction

TOVs in electrical transmission and distribution networks result from the unavoidable effects of lightning strikes and network switching operations. A TOV can be defined as the response of an electrical network to a sudden change in network conditions, either intended or accidental, (e.g. a switching operation or a fault) or network stimuli (e.g. a lightning strike). A transient is a natural part of the process by which the power system moves from one steady state condition to another [2]. Its duration is in the range of microseconds to milliseconds. A brief explanation and analysis of transients can be found in references [3, 4]. In this chapter, the fundamental concepts of TOVs with especial emphasis on switching transients is presented to facilitate understanding of the next chapters as the transients dealt with in this work are of this type caused by switching operation of VCBs.

2.2 Classification

TOVs are broadly classified as impulsive and oscillatory.

(1) Impulsive transients

The most common cause of impulsive transients is lightning. Lightning is associated with the discharge of a large current. This current can reach up to 200kA. The overvoltage developed in this case is limited by the impedance of the system seen by the lightning current. This overvoltage can reach several MV. This situation usually causes power system faults due to insulation failure which in turn causes a supply interruption and voltage sags throughout the distribution network.

Impulsive transients are characterized by their rise and decay time and peak values. Lighting current and its corresponding voltage rises to its peak in a time which varies from less than a microsecond to 10 or 20 microseconds and then decays in a few hundred microseconds [3].

(2) Oscillatory transients

Switching operations within the network are a major cause of oscillatory overvoltage transients. Such operations include switching of circuit breakers to clear faults, switching

of utility capacitor banks and switching of distribution feeders to rearrange the network for maintenance or construction.

A switching overvoltage or as they are some times called switching surge is generated due to the interaction of the inherent elements(inductance, capacitance and resistance) associated with an electric network .When current flows through an inductance, it produces magnetic flux. Any effort to change the magnetic flux (i.e. the current) will be opposed by the inductance, which is manifested by the generation of a counter EMF in the inductance in such a direction as to keep the magnetic flux (and the current) in the inductance constant. Therefore, when a circuit breaker tries to interrupt a current, a voltage is developed by the system inductance to oppose the change in current. The faster a switch tries to interrupt a current, the higher the resulting switching surge voltage is. Theoretically this voltage can be infinite if the current through the inductor is snapped off instantaneously. However, as every electrical system can withstand a maximum level of voltage, the system maximum voltage strength is reached causing a discharge and a temporary or a permanent damage. In practice, all electrical systems have capacitances. When the current is interrupted in an electrical system, the current through the inductance flows through the capacitance, thus transferring the energy from the inductance to the capacitance. The energy originally stored in the inductance is transferred back and forth until it is finally damped by the system resistance.

In a system with large physical extension, such as a power transmission line where the inductance and the capacitance are distributed, traveling voltage and current waves are generated during a switching operation. Dangerously high voltages can be generated by multiple reflections at the end of the line.

2.3 Shunt Capacitor Switching Transients

Shunt capacitors are used extensively in power transmission and distribution systems as a means of supplying reactive power for voltage support. These capacitors are implemented in the system in order to control the system voltage, to increase the power transfer capability, to reduce equipment loading, and to reduce energy costs by improving the power factor of the system. They are switched in and out depending on the level of support needed. When a discharged capacitor is energized, the voltage of the bus bar to which it is attached will momentarily collapse as the voltage across a capacitor can not change instantaneously. This is followed by an oscillatory transient recovery voltage which can be as high as 2p.u. An example of a capacitor switching waveform is shown in Fig.2.2. The same effect can occur when a capacitor is switched off and a re-strike occurs (i.e. the circuit recovery voltage causes the dielectric between the switch contacts to break down and capacitor current is reestablished). Capacitor switching transients can be magnified to quite high values as they pass to a lower voltage level if certain network conditions are met. This can occur when transients originating in the medium voltage (MV) distribution network move into the low voltage (LV) network and there are power factor correction (PFC) capacitors present at LV consumer's installations. Such a situation is given in *Fig. 2.1* which shows an MV/LV network supplied by an MV feeder

with inductance L_1 . A switched capacitor C_1 is connected to the MV bus bar. The series combination of the outgoing MV feeder and the MV/LV transformer has an inductance of L_2 . The PFC capacitor C_2 is connected to the LV bus bar. Magnification occurs when the predominant frequency of the switching transient is approximately equal to the resonant frequency of the LV system. This condition is mathematically represented by

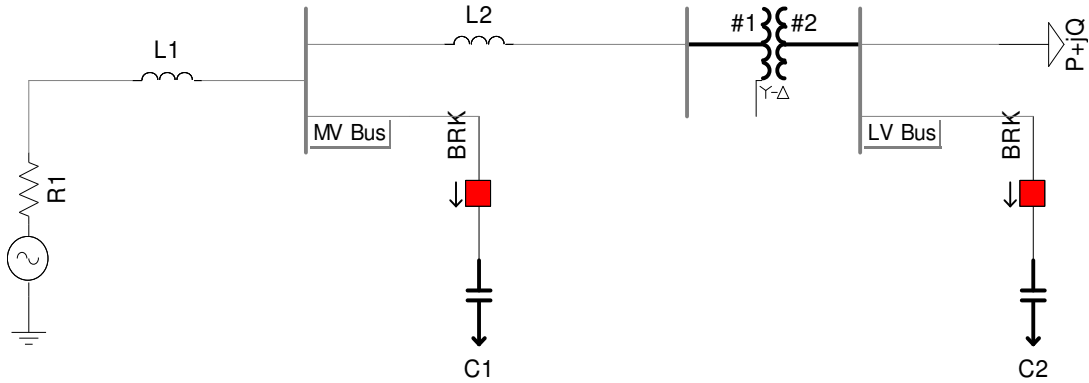


Fig.2.1 Power system network used in PSCAD/EMTDC to illustrate magnification of capacitor switching transients.

$$L_1 C_1 \cong L_2 C_2 \quad (2.1)$$

where L_1 is the system source inductance seen from MV bus bar, C_1 is the capacitance of switched capacitor, L_2 the inductance of step-down transformer and associated MV feeder and C_2 is the capacitance of LV PFC capacitor.

The overvoltage associated with this phenomena can reach to a peak value up to 4 times the corresponding power frequency system voltage.

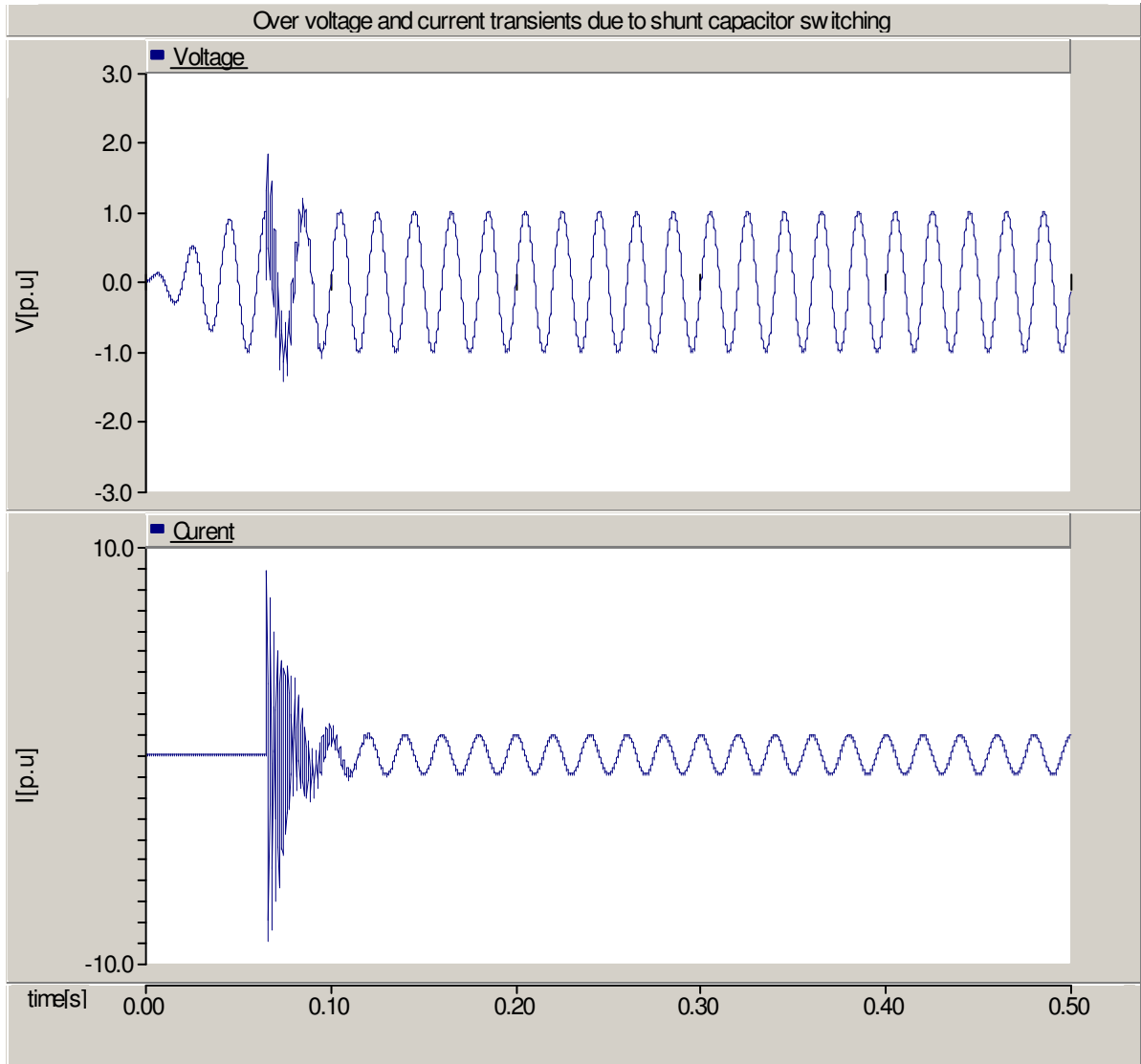


Fig.2.2 Voltage and current resulting from capacitor switching simulated.

2.4 Traveling Waves

The parameters of transmission lines, cables, as well as transformer and generator windings are distributed. A characteristic of a circuit with distributed parameters is its ability to support traveling transient waves of voltage and current. The influence of the distributed parameters on the propagation of TOV depends on the frequency content of the waves. Higher frequency transients will be more affected by the stray and distributed inductance and capacitance of the system than lower frequency transients.

The current and voltage waves travel in both directions from the point of excitation or disturbance. The ratio of the amplitudes of the voltage and the current waves on a

transmission line or cable is called the characteristic impedance Z_0 of the line and is for a lossless line given by

$$Z_0 = \sqrt{\frac{L}{C}}, \Omega \quad (2.2)$$

where L and C are the distributed inductance and capacitance respectively of the line or cable. Typical values of the characteristic impedance vary between 300 to 500 Ω for overhead lines and for cables from 30 to 60 Ω [2].

The velocity of propagation of the waves for a lossless line is given by

$$v = \sqrt{\frac{1}{LC}}, \text{ m/s} \quad (2.3)$$

and depends on the medium of propagation. It is near the speed of light (3×10^8 m/s) for overhead lines, and between one half and two thirds of this value for underground cables [2].

Like all other waves, traveling waves initiated by disturbances in power systems also have classic wave characteristics like reflection and refraction.

Reflection and refraction of traveling waves

When voltage and current waves propagate in transmission lines or cables, there is a strict proportionality between the two. The proportionality constant is the characteristic impedance of the line or cable. When a wave arrives at a point of discontinuity, which could be an open end, an underground cable or transformer, where the characteristic impedance changes, to keep this proportionality, two new wave pairs are generated, one reflected back superimposed on the incident wave and another transmitted beyond the discontinuity. The amplitudes of the reflected and refracted waves are such that the voltages to current proportionalities are preserved for each.

The consequence of these discontinuities could be the production of complex sets of traveling waves which add and subtract, possibly causing quite high voltages at some points.

The magnitudes of the reflected and refracted voltage waves at a junction point with characteristic impedances Z_a and Z_b on the incident side and refractive side, respectively, can be quantified as

$$V_2 = \frac{Z_b - Z_a}{Z_a + Z_b} V_1 \quad (2.4)$$

$$V_3 = \frac{2Z_b}{Z_a + Z_b} V_1 \quad (2.5)$$

where V_1 is the incident wave, V_2 is the reflected wave and V_3 is the refracted (transmitted) wave. $\frac{Z_b - Z_a}{Z_a + Z_b}$ is called the reflection coefficient and $\frac{2Z_b}{Z_a + Z_b}$ is the refractive coefficient.

The reflected and transmitted currents are given by

$$I_2 = -\frac{V_2}{Z_a} \quad (2.6)$$

$$I_3 = -\frac{V_3}{Z_b} \quad (2.7)$$

Chapter 3

CABLE MODELING

3.1 Introduction

This chapter treats modeling of a real power cable in PSCAD/EMTDC. The objective is to find a close representation (model) of a real cable that best depicts its response. The model can then be used to study the effect, at a wider range of frequencies, of different network operations (both normal and abnormal) in a real medium voltage power network of which the cable is a part. A model is developed in PSCAD/EMTDC which suitably works not only at power frequency but also at higher frequencies. The focus is on high frequency effects like EM transient propagation, reflections, skin effect, etc. Both single phase and three phase cables have been modeled. These models are later to be used to simulate and study effects of TOVs in real power networks during switching operations, earth faults, etc.

It can be sufficient to model a power cable by using simple RLC Π -network to study its response at a single frequency such as steady state. However, for higher frequencies, frequency-dependent models where the frequency dependence of the distributed cable parameters such as capacitance, inductance and resistance per meter are well accounted for should be used to include high frequency consequences such as skin effect, etc.

PSCAD/EMTDC provide three options for modeling of a power cable [11]:

i) Bergeron model

This model treats the cable as an infinite number of Π sections of L, R, and C. It represents accurately only one frequency.

ii) Frequency dependent (mode) model

This model represents well the frequency dependence of the distributed parameters over a wide range of frequencies, but uses a constant transformation of internal matrices. Thus, it may not be good if the conductors are not ideally transposed.

iii) Frequency dependent(phase) model

This model also represents well the frequency dependence of the distributed parameters over a wide range of frequencies. The frequency dependence of

internal transformation matrices is well taken care of. This model is, therefore, the best of all three. This model has been used in our work.

3.2 Cable Parameter Selection in PSCAD/EMTDC

The basic parameters used to represent cables and transmission lines are series impedance matrix Z and shunt admittance matrix Y [9], [10].

$$Z(\omega) = R(\omega) + j\omega L \quad (3.1)$$

$$Y(\omega) = G(\omega) + j\omega C \quad (3.2)$$

where R , L , G , C are series resistance, series inductance, shunt conductance and shunt capacitance respectively. Both Z and Y are functions of frequency ω . All the commonly used programs for simulation of transients, EMTP-type programs including PSCAD/EMTDC have dedicated support routines for calculating an electrical representation of cable system in terms of the series impedance matrix Z and admittance Y [9], [10].

In PSCAD/EMTDC the cable parameters are calculated based on the geometry and material property of the cable specified by the user. There is a major difference, however, on the geometric representation of the actual cable from that used in PSCAD/EMTDC as the later does not account for the presence of a semiconducting screen that is present in the actual cable and it assumes that the core conductor is a homogeneous solid conductor which is different from the core conductor made up of many strand conductors in the actual cable. The situation is further complicated by the fact that some of the geometrical dimensions of the cable are not given by the manufacturers. *Fig.3.1* below shows the difference between the actual cable and its representation in PSCAD/EMTDC.

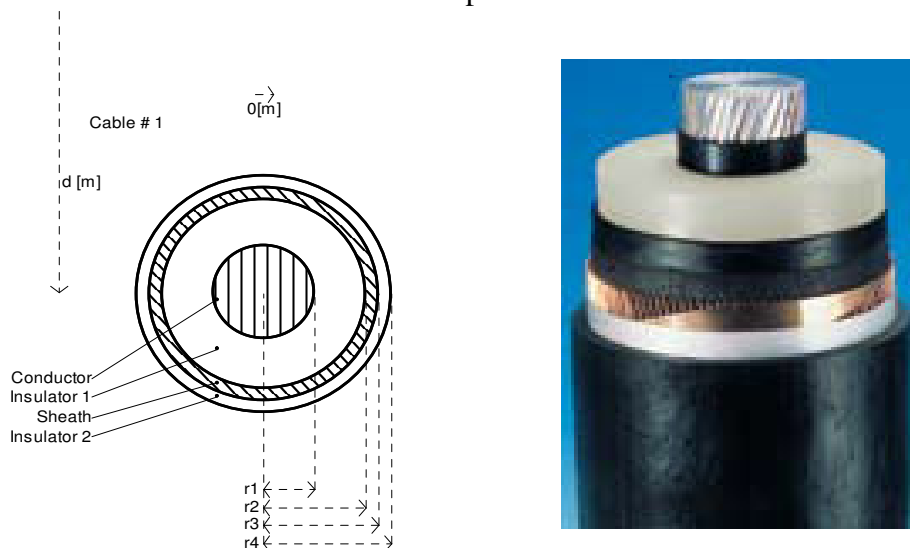


Fig.3.1 Actual cable versus PSCAD/EMTDC representation.

As it is clearly shown in *Fig.3.1* PSCAD/EMTDC requires the geometric parameters for the core, semiconductor and sheath. An actual cable however includes a conductor, an

inner semiconducting screen insulator, an outer semiconducting screen sheath among others. Accordingly the user needs to decide how to represent the following cable features which PSCAD/EMTDC fails to represent.

- 1) Core stranding
- 2) Inner and outer semiconductor layers
- 3) The wire screen

The following sections are dedicated to obtaining the cable parameters for simulation in PSCAD/EMTDC. An attempt will be made to represent the above features.

3.2.1 Core Parameters

The main parameters of the core to be given to PSCAD/EMTDC are the resistivity and radius. The actual cross section area of the core given by the manufacturer is different from the area of circle obtained using the radius of the conductor given by a manufacturer for stranded core design. It is obvious that the area of the core needed for resistance calculation in PSCAD/EMTDC is obtained based on the radius specified, hence there is a need to make some form of correction to account for the fill factor as to give the correct resistance of the conductor. Stranded conductors can be modelled in PSCAD/EMTDC in two different ways. The first way is to model it as a solid conductor by increasing the resistivity ρ by a factor equal to the inverse of the fill factor as given by the formula below

$$\rho' = \rho \frac{\pi r_1^2}{A_c} \quad (3.3)$$

where ρ' is the corrected resistivity to account for the space between the strands, ρ is the resistivity of the core material, r_1 is the radius of the conductor given by manufacturer, and A_c is the efficient cross section area of the core.

The second way is to model it as a hollow cylinder whose cross section is the difference of areas between two circles with area equal to A_c as shown by *Fig.3.2*.

The inner radius in this case is given by

$$r_{in} = \sqrt{r_1^2 - \frac{A_c}{\pi}} \quad (3.4)$$

If the manufacturer provides the DC resistance for the core R_{DC} , the corrected resistivity can alternatively be calculated as

$$\rho' = R_{DC} \frac{\pi r_1^2}{l} \quad (3.5)$$

where l is cable length. Resistivity of commonly used core materials is given in Table 3.1.

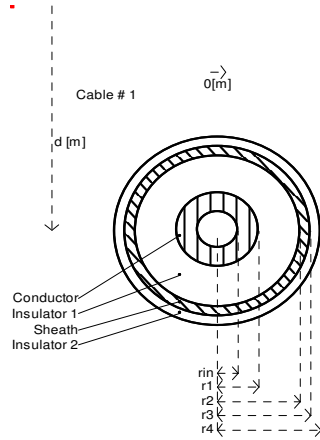


Fig.3.2 Alternative approach of dealing with stranding of core.

Table 3.1 Resistivity of commonly used core material.

MATERIAL	COPPER	ALUMINIUM
$\rho[\Omega.m]$	$1.72E^{-8}$	$2.82 E^{-8}$

3.2.2 Insulation and Semiconducting screen

The main insulation of high-voltage cables is always sandwiched between two semi conductive layers. Unfortunately, none of the EMTP-type programs for instance PSCAD/EMTDC in our case allows the user to directly specify the semiconducting layers [9], [10]. These must therefore be introduced by a modification of the input data. As explained in [9] and [10], this is done by allowing the insulation to extend between the core conductor and sheath conductor, and increasing the permittivity proportionally to leave the capacitance unaltered. This data conversion procedure is summarized as follows.

- 1) Calculate r_2, r_1 plus the sum of the thickness of the semi conducting screens and the main insulation. This radius is given as outer radius of the insulation to PSCAD/EMTDC.
- 2) Calculate the corrected permittivity ϵ_{r1} as

$$\epsilon_{r1} = \frac{C \ln(r_2 / r_1)}{2\pi\epsilon_0} \quad (3.6)$$

where C is the cable capacitance and $\epsilon_0 = 8.854E^{-12}$.

If the capacitance is unknown, the permittivity is corrected as

$$\epsilon_{r1} = \epsilon_{rins} \frac{\ln(r_2 / r_1)}{\ln(b / a)} \quad (3.7)$$

where a and b are the inner and outer insulation radii respectively and ϵ_{rins} is the permittivity of the insulation material.

3.2.3 Sheath conductor

PSCAD/EMTDC allows the user to specify the sheath conductor. When the sheath conductor is made of wire screens, as it is the case with the cable we are dealing with, the best way to model it is with a tubular conductor having a cross section area equal to the total wire area A_s , inner sheath radius of r_2 and outer radius r_3 given by

$$r_3 = \sqrt{\frac{A_s}{\pi} + r_2^2} \quad (3.8)$$

The other input data that needs to be specified to PSCAD/EMTDC that is worth mentioning is the resistivity of the sheath material. Materials commonly used as sheath conductor along with their resistivity is given in Table 3.1.

3.3 Testing Model

The cable models developed in the foregoing sections are tested to characterize different frequency dependent effects like EM propagation, damping (due to skin effect and proximity effect) and reflections. The cables at the wind cable lab were charged to 800V and discharged through a COM-gap to excite a very steep fronted voltage at one end and measure the transients at the other end for different lengths and arrangements of the cable system. The measured waveforms are compared with results obtained by simulating the same operations using the frequency-dependent cable models developed in 3.2 using PSCAD/EMTDC.

3.3.1 Measurement Set-Up

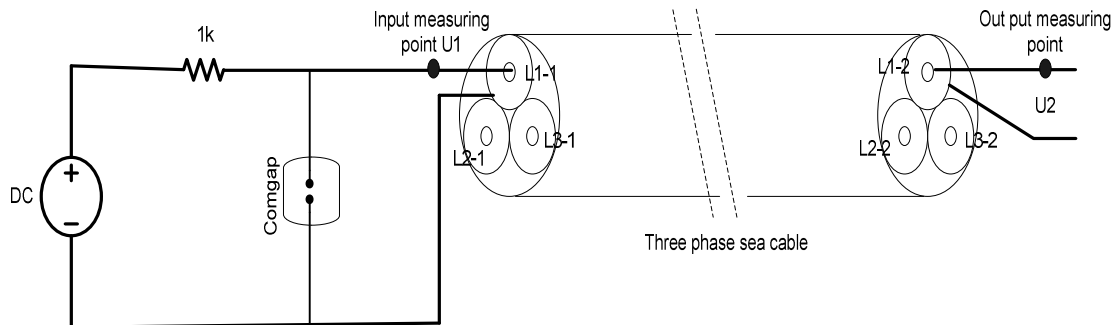


Fig.3.3 Experimental set up for cable discharge with step.

The experimental set up is based on a variable DC source, a current limiting resistor of 1k Ω , ELFA AC240 comgap (see Table 3.3), and LeCroy Oscilloscope for measuring waveforms(see Table 3.2). The cable was charged by increasing the variable DC voltage source until the comgap break down and then the cable is discharged through the comgap. In other words, a step excitation is applied between core conductor and the sheath when the gap discharges, which propagates on to the other end of the cable until it is finally damped by the system resistance. In the set up shown in *Fig.3.3* U1 and U2 represent the input and out put measured points.

The experiment was done on a 620m cable while it was rolled on drum (see *Fig. 3.4*) and on cable sections with 242m and 484m lengths of the cable lab set up after the cable had been cut and installed.The specifications of the cable is given in Table 3.4

Table.3.2 Specifications of LeCroy 9354A Digital Oscilloscopes.

BANDWIDTH	500MHZ
Channels	4
Sample Rate	2GSa/sec
Memory Depth	50K pt/sec
Sensitivity	2 mV/div to 5V/div
Number of Bits 8	8 bits
Input Impedance	1 MOhm/14pF or 50Ohm \pm 1%
Main time base lowest	1 ns/div

Table.3.3 ELFA AC240 Comgap product specification.

PARAMETER	MINIMUM	MAXIMUM
DC Breakdown Voltage	425V	-
Impulse Breakdown Voltage		800V
Insulation Resistance	10 ¹⁰ Ω	
Capacitance		1PF
Operational Temperature	-40°C	+125°C
AC Follow-On Current	>300A	

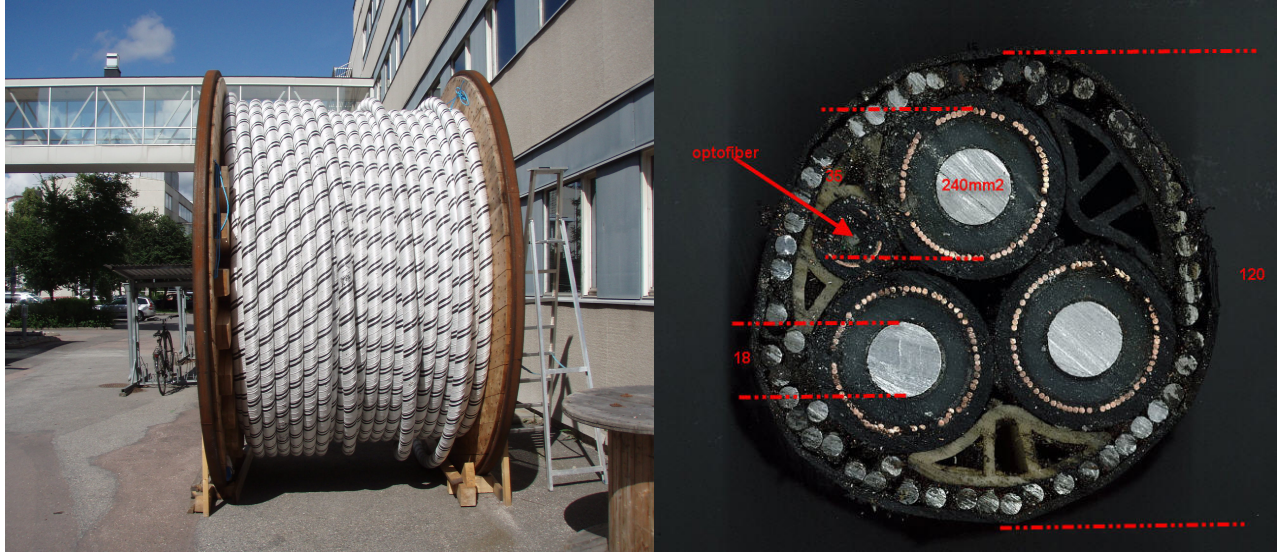


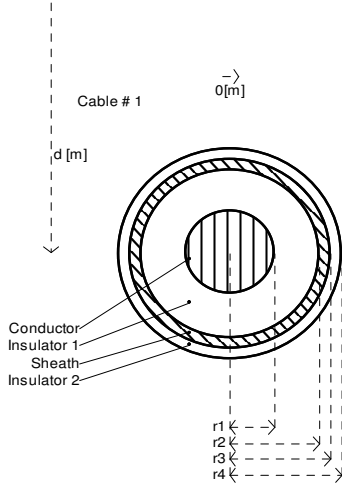
Fig.3.4 three phase 24 kV 620m Sea cable on drum and its cross section.

Table.3.4 Specification three phase sea cable.

CORE MATERIAL	ALUMINIUM SOLID CONDUCTOR
Core cross section	240mm ² /phase
Core radius	9mm
Main insulation material	Mainly of PE
Screen conductor	Copper
Screen cross section	85mm ²
Armor material	Steel

	MATERIAL	CROSS SECTION AREA [mm ²]	RADIUS [mm]	THICKNESS [mm]
Core	Aluminum	3x240	9	
Main insulation	XLPE			6
Outer insulation			22.5	
Inner/outer semiconducting screen				0.5/1
Sheath conductor	Copper	3x98		

The experimental set up in Fig.3.3 was simulated in PSCAD and the cable was modeled according to the modeling procedure given in section 3.2. The parameters of the cable model are accordingly given below.



$$r_1 = 9\text{mm}$$

$$r_2 = r_1 + \text{Main insulation thickness} + \text{sum of inner and outer semiconducting screen thickness}$$

$$r_2 = 9\text{mm} + 6\text{mm} + 0.5\text{mm} + 1\text{mm} = 16.5\text{mm}$$

$$r_3 = \sqrt{\frac{A_s}{\pi} + r_2^2} = \sqrt{\frac{85\text{mm}^2}{\pi} + (16.5\text{mm})^2} = 17.3\text{mm}$$

$$a = r_1 + \text{thickness of inner semiconducting screen}$$

$$a = 9\text{mm} + 0.5\text{mm} = 9.5\text{mm}$$

$$b = a + \text{main insulation thickness}$$

$$b = 9.5\text{mm} + 6\text{mm} = 15.5\text{mm}$$

$$\text{Corrected permittivity } \epsilon_{r1} = \epsilon_{rins} \frac{\ln(r_2 / r_1)}{\ln(b / a)} = 2.85$$

$$r_4 = 22.5\text{mm}$$

3.4 Results and Analysis

When a cable is energized with a fast fronted impulse, a traveling wave is likely to be incepted. One important requirement for the formation of traveling waves is that the duration of the wave should be significantly less than the time taken to traverse the medium. Some characteristics inherent to traveling waves in cables and transmission lines are reflections, propagation delay and damping.

The waveforms in Fig.3.5 and 3.7 show the results of the experimental tests for two different cable lengths. Fig.3.6. and 3.8 are results of simulations in PSCAD/EMTDC using the frequency dependent cable model. Subsequent Figs 3.9 and Fig3.10 are “zoom ins” of these in order to show the pulses more clearly.

The shorter the cable length, the more frequent reflections the cable accommodates and the higher the frequency of the pulses. This can be observed in Fig 3.9(a) and Fig.3.10 (a) which present the measured waves at the end of a 242m and 484m cables. The frequency of oscillation for the 242m cable is approximately 154kHz which is almost double that for the 484m cable which is 76.7kHz. The traveling time of the reflected waves between the discharging COM-gap and the cable open ends also becomes shorter for the shorter cable since the propagation velocity for the same type of cable is identical whatever the length is. This is demonstrated by the results in Fig 3.9(a) and Fig.3.10 (a). The traveling time is equal to a quarter of the propagating pulse cycle. The propagation delay for waves to reach the open end of the 242m cable has been measured to be 1.634us

delay for waves to reach the open end of the 242m cable has been measured to be 1.634us and is 3.26us for the 484m cable. The cable oscillation frequency indirectly affects the damping of the propagating transient due to the conductor ac resistance being increased by the skin effect. Thus, damping of the waves increases with frequency. This can be seen in the same figure where we have quicker dying of the reflected waves on the 242m cable than on 484m cable due to higher frequency.

Similar results are obtained by simulating the same operations on the cables using the frequency dependent model in 3.2. *Fig 3.9(b)* and *Fig.3.10 (b)* signify a higher frequency of oscillation, shorter propagation delay and faster damping for the 242m than for 484m cable. Comparable figures are also found for the pulse frequency and propagation time which are in reasonable agreement with those found in the measurements. Measured and simulated values are given in Table 3.5 for comparison.

Similar results are found by computing the above parameters from the propagation velocity of the cables. The propagation velocity can be calculated from the inductance L and capacitance C per meter of the cable as given in (2.3) and L and C have been calculated from the cable property and geometry (see section 3.3.1) to be 0.121nH/m and 0.269nF/m respectively yielding

$$v = \sqrt{\frac{1}{0.121\text{nH/m} * 0.269\text{nF/m}}} = 175\text{m/us} .$$

This gives a traveling time of

$$T_p = \frac{S}{v} \tag{3.9}$$

where S is the length of the cable yielding

$$T_p = \frac{242\text{m}}{175\text{m/us}} = 1.38\text{us}, \text{ for the 242m cable length and}$$

$$T_p = \frac{484\text{m}}{175\text{m/us}} = 2.76\text{us}, \text{ for the 484m cable length}$$

It should be noted that the oscillation frequency is slightly higher in the simulations. One source of this error could be due to the additional capacitance to ground from the measuring probes which may have decreased the frequency in the measurements as $f_0 = 1/2\pi\sqrt{LC}$ where f_0 is the oscillation frequency.

Table.3.5 Comparison of measured and simulated values.

Cable length	Oscillation freq. (Simulation) [MHz]	Oscillation freq. (Measurement) [MHz]	Travel Time (Simulation) [us]	Travel Time (Measurement) [us]
242m	0.181	0.154	1.4	1.634
484m	0.08962	0.0767	2.789	3.26

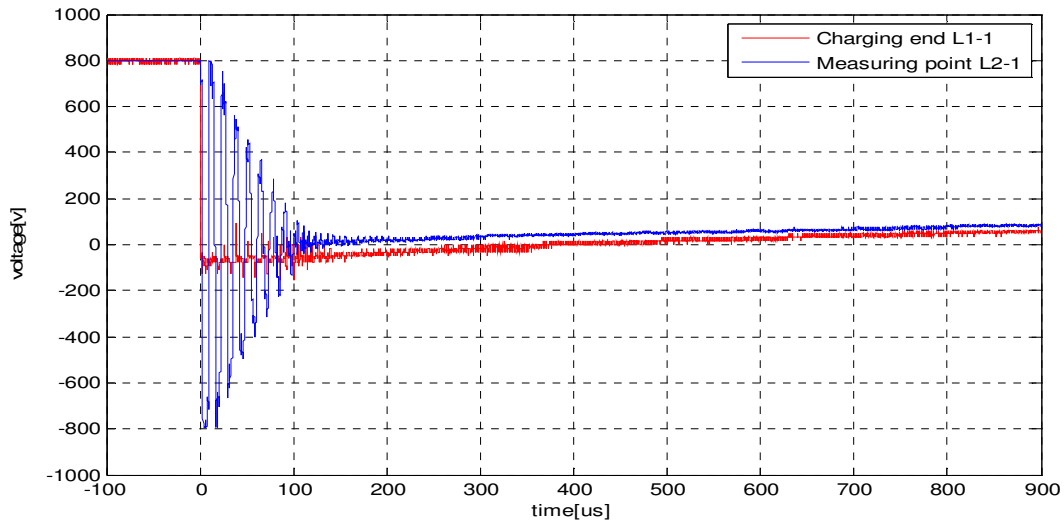


Fig.3.5 Cable energizing at L1-1 and measuring point at L2-1 (measured).

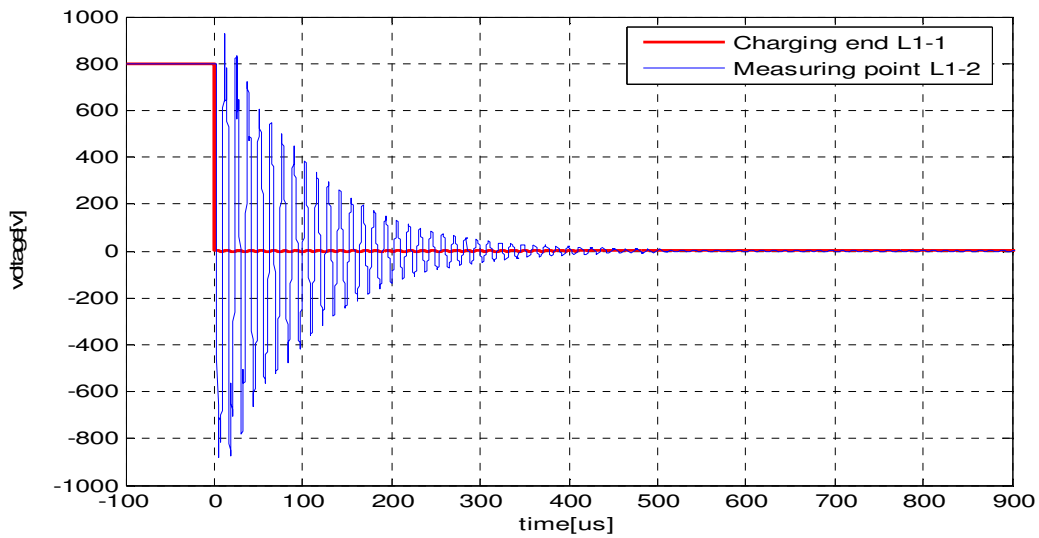


Fig.3.6 Cable energizing at L1-1 and measuring point at L2-1 (simulated).

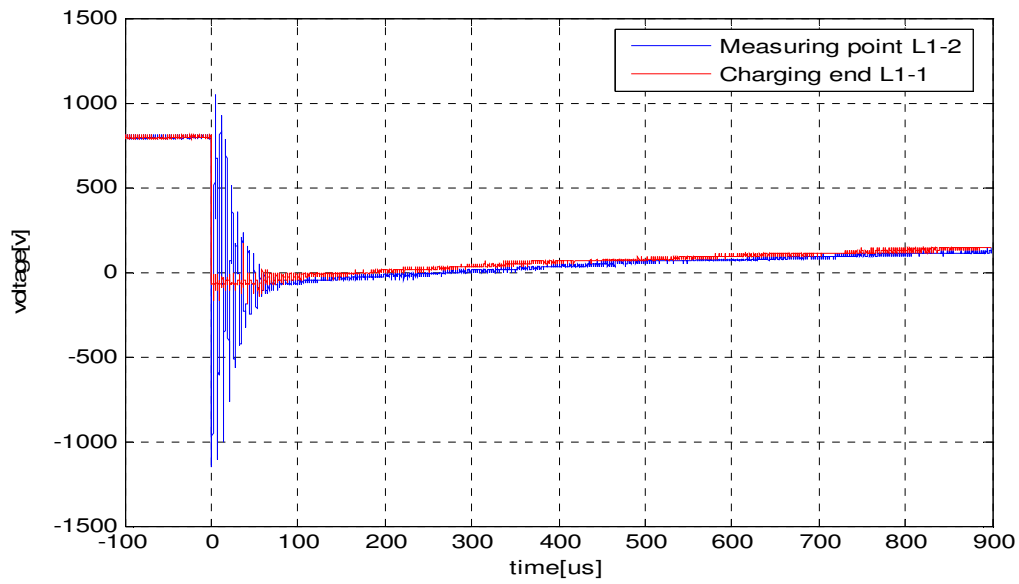


Fig. 3.7 Cable energizing at L1-1 and measuring point at L1-2(circuit breaker end) measured.

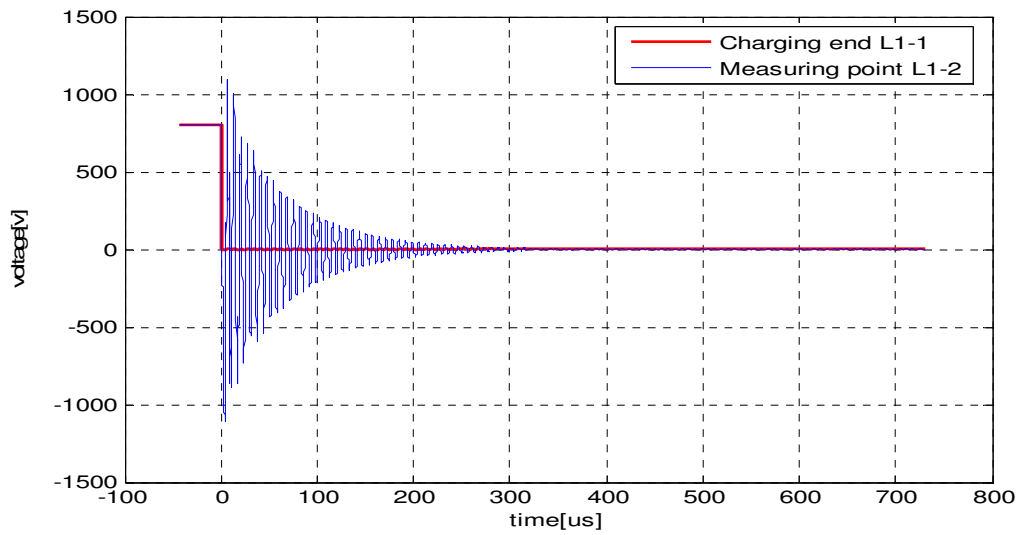


Fig.3.8 Cable energizing at L1-1 and measuring point at L1-2(circuit breaker end) simulated.

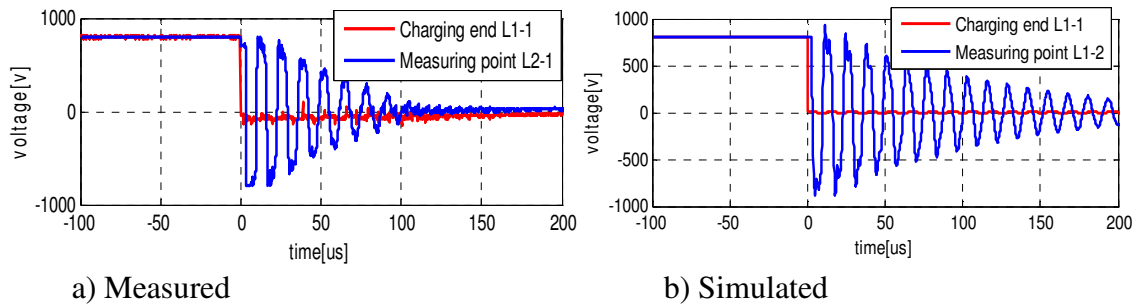


Fig.3.9 Measured and simulated waves for $L=484m$ ($T_s=0.02us$).

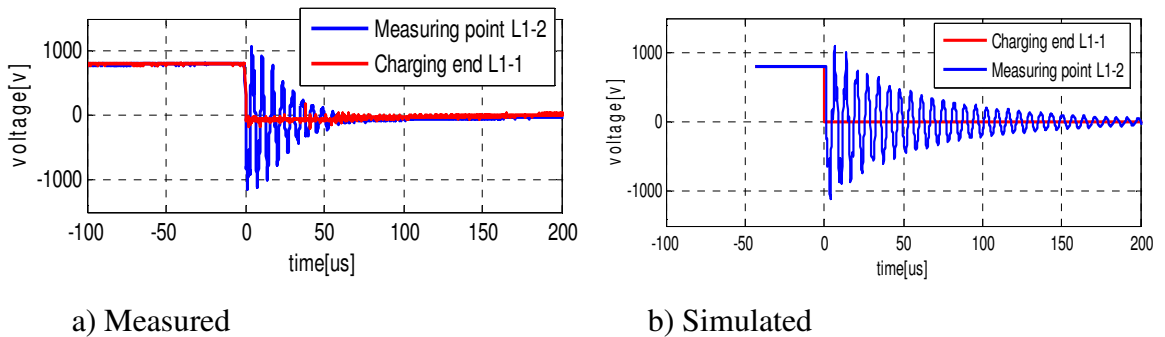


Fig.3.10 Measured and simulated waves for $L=242m$ ($T_s=0.02us$).

3.5 Conclusions

- ✚ Of the three frequency dependent cable models provided in PSCAD/EMTDC, the Frequency Dependent (phase) Model is the best model. It was used with certain adjustments on data entered to account for the presence of semiconducting layers, and core and/or sheath stranding.
- ✚ The results of the experiment show that good agreements have been achieved between measured and simulated values in the frequency of oscillation and propagation delay validating the cable model proposed in this regard.
- ✚ Small disagreements in these parameters are, however, noticed and the authors believe they can be due to unaccounted capacitance of the measuring cables and additional stray capacitances and inductances in the real system.
- ✚ Although it has been found that both simulations and measurements show an increase in damping of the EM transients with increasing frequency of oscillation as should be, quicker damping is observed in reality than in the simulations. This is either the simulation model does have certain parameters estimated incorrectly or the real system has additional resistance or conductance elements than considered in the model.

Chapter 4

VCB MODELLING

4.1 Introduction

At transmission level, the most modern switching devices used are SF6 breakers, while at medium voltages VCBs are primarily used [20]. VCBs have very suitable properties like capability of interruption of both power frequency and high frequency currents, and good gap breakdown voltage recovery properties. Their ability to interrupt these high frequency currents, however, may lead to multiple gap breakdowns (re-ignitions) which may be the cause for very severe overvoltages under certain network conditions. Many MV component failures have been found to be caused by TOVs due to VCBs. A good model that replicates the VCB characteristics like current chopping capability, dielectric breakdown strength and high frequency current quenching capability is therefore crucial to study in order to understand the occurrence of these TOVs. This chapter deals with the general theory of modeling a VCB in PSCAD/EMTDC that takes into account the above characteristics. A VCB for use in MV networks as wind parks has been modeled based on [16], [17]. The breaker model is then used in a test circuit to see if it actually characterizes the original VCB properties stated above.

4.2 Phenomena causing over voltages in VCB

There are four reasons why overvoltages occur in vacuum circuit breakers: current chopping, multiple re-ignitions, virtual current chopping and pre-strikes [13].

4.2.1 Current chopping

If the contacts of a VCB start opening close to a zero of a power frequency current, the arcing current across the contacts becomes unstable as to be extinguished. Detailed treatment of this instability can be found in [18]. This behavior of the breaker to interrupt a small but non zero current just before the zero of a power frequency current is called current chopping. The mean value of the chopping current depends on the contact materials, the level of the load current, and the instant of contact separation. After the current is chopped and the arc is extinguished, a transient recovery voltage (TRV) appears across the VCB contacts. The shape and level of the TRV depends on the actual chopping current and the resulting capacitance, inductance and resistance on the load

side. Higher chopping current produces higher TRV as do high inductance on the load side. (4.1) shows how the chopping voltage (TRV) is related to the inductance and the chopping current. If the TRV developed becomes greater than the dielectric strength of the breaker, the gap may reignite.

$$U_{ch} = i_{ch} \sqrt{\frac{L}{C}} \quad (4.1)$$

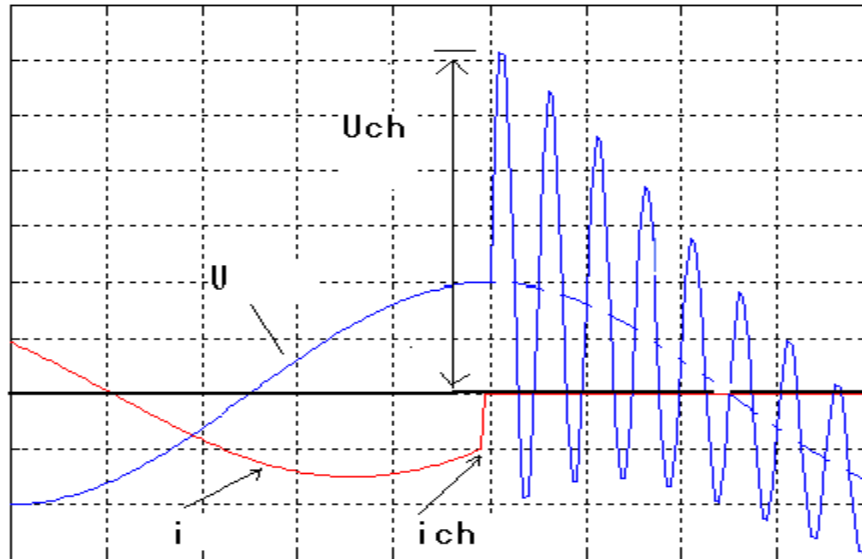


Fig.4.1 TRV waveform and chopped current.

4.2.2 Voltage Escalation

After the extinction of the arc at current zero of the power frequency current, a race begins between the TRV developed between the breaker contacts and the dielectric strength of the gap. If the chopping happens very close to current zero, the gap separation by the time the arc has extinguished is small; the dielectric strength of the gap is, therefore, accordingly small. The TRV may in this case exceed the gap voltage strength and the gap may re-ignite and start conducting. This arcing current is of very high frequency superimposed on the line frequency current. If the high frequency current is higher or equal to the power frequency current in magnitude, they may add up to cause several high frequency arc current zeros through the breaker. The VCB may be able to interrupt this current at one of the zeros if certain conditions are met. Again, if the TRV exceeds gap breakdown strength, a re-strike occurs causing a substantially high frequency current. This process may repeat until the gap can withstand the TRV. Each subsequent re-strike produces higher and higher load side over voltages due to the increased and continuous transfer of energy between the inductance and the capacitance on the load side

due to the re-strike and extinction respectively, as shown in *Fig.4.2*. This process of growth of TRV is termed as voltage escalation.

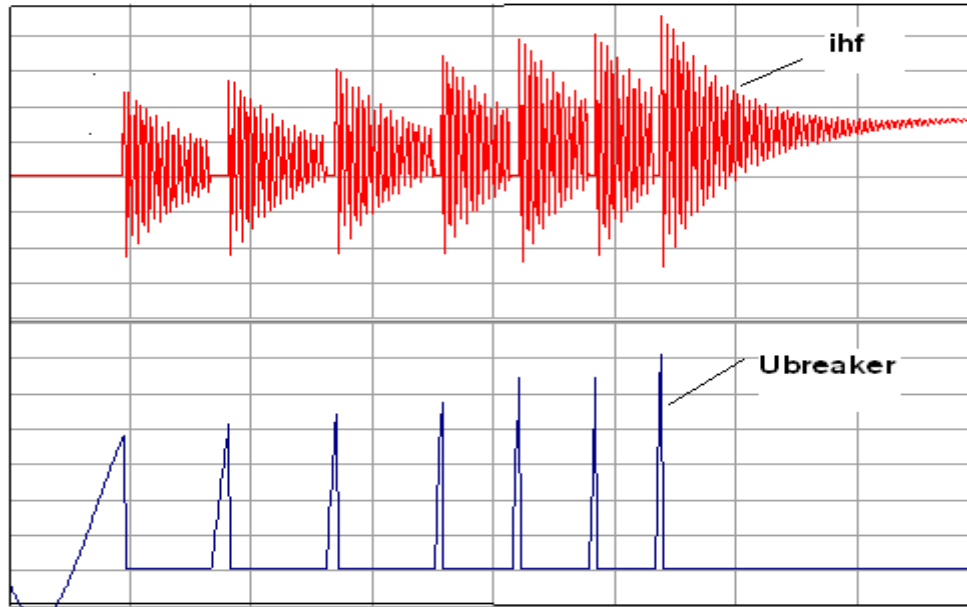


Fig.4.2 Restrike currents and voltage escalation.

4.2.3 Virtual Current Chopping

In three phase circuits, the flow of the high frequency currents due to ignition in one of the phases can lead to injection of the current into the other phases through inductive and capacitive coupling and can lead to forced current zeroes in these phases [16]. This mechanism is called virtual current chopping when re-ignitions occur due to these current zeroes. What happens is if the magnitude of the high frequency current that couples to the other phases is higher than the peak of the line frequency current, the current in the phases will pass through zero several times before its natural zero. This may cause several re-ignitions and interruptions escalating the voltage. Compared to normal current chopping, virtual current chopping can be much higher, as high as several hundred amperes compared to 3 or 4A [17].

4.2.4 Prestrikes

While re-ignitions are for opening breakers, pre-strikes are for closing breakers. Before the contacts come to a physical contact, during closing, the voltage between the contacts may get higher than the dielectric withstand voltage of the gap which diminishes as the contacts get closer. In this case, the gap breaks down before the contacts are actually

closed and an arcing current is established, and a prestrike is said to have occurred. Depending on the external network parameters, a high frequency arcing current can occur with several zero crossings. Multiple pre-strikes might happen if the breaker is able to interrupt some of these and the process repeats. Consequently, multiple high slope transient step voltages are produced.

4.3 Modeling of VCB

In simulating a network for transient study, the components involved should be accurately modelled. However obtaining accurate VCB Model which simulates all the phenomena discussed above is difficult. For one thing these phenomena are statistical in nature and secondly the authors believe it is beyond the scope of this paper as modelling all of those phenomena is a thesis work by itself.

The generic model incorporates different stochastic properties inherent to the breaker operation to control the actual state of the breaker. The properties are as specified in [19]:

- Random nature of arcing time
- Current chopping ability
- The characteristic recovery dielectric strength between contacts when opening
- High frequency quenching capability at current zero.

The model introduced in this paper is similar to the models on references [16, 17, and 19]. It simulates the following phenomena:

1. Current chopping
2. Dielectric strength
3. High Frequency quenching capability

4.3.1 Current chopping

The actual chopping current is non-deterministic. However earlier research established different mean chopping levels [19] for different load currents and contact material. The mean chopping current I_{CH} is estimated by (4.2) according to [19]:

$$I_{CH} = (\omega \cdot \hat{I} \cdot \alpha \cdot \beta)^q \quad (4.2)$$

where $\omega=2\pi f$ is angular frequency of power supply, \hat{I} =Amplitude of the 50Hz current, α , β , q are parameters dependent on contact material. For modern VCBs which use Cu/Cr contact these constants are given by

$$\alpha=6.2 \times 10^{-16}$$

$$q = (1 - \beta)^{-1} = -0.07512$$

$$\beta=14.3$$

To account for the statistical nature of the chopping current, the mean chopping current determined by (4.2) is varied by a normal distribution curve with a standard deviation of 15%.

4.3.2 Dielectric strength

In modelling the breakdown strength of the contact gap, the cold gap breakdown is considered in this paper as this is the relevant breakdown strength when the preceding arc current does not exceed several hundred Amperes. The cold withstand voltage characteristic of the VCB is function of the contact distance. It is strongly dependent on the speed of contact separation. For short gaps linear variation of dielectric strength with distance can be assumed [14].

$$U_{bd} = A(t - t_0) + B \tag{4.3}$$

where t_0 is moment of contact opening, A and B are constants. The constant A is the rate of rise of dielectric strength. The values of the constants A and B in (4.3) for three different typical dielectric strength characteristics are shown in Table 4.1, as proposed by [14]. However those parameters can be adjusted later using experimental data of the VCB.

The value of the dielectric strength so calculated is assumed as the mean value of a Gaussian distribution with a standard deviation of 15% as break down phenomena are statistical in nature.

Table 4.1 Constants for equation (4.3) (Reproduced from [14]).

BREAK DOWN VOLTAGE TYPE (BV TYPE)	A(V/MS)	B(KV)
High	17	3.4
Medium	13	0.69
Low	4.7	0.69

4.3.3 High Frequency Quenching Capability

When the transient recovery voltage developed across the breaker exceeds the dielectric withstand voltage, re-ignition occurs. High frequency current superimposed on power frequency will be conducted through the breaker. VCBs are capable of interrupting this high frequency current at one of the zero crossings. However, successful interruption depends on the rate of change of this current at current zero. Interruption of the high frequency current will not occur if the rate of change at current zero is higher than the critical value of quenching capability given by (4.4) [14,16,17,19]

$$\frac{di}{dt} = C(t - t_0) + D \quad (4.4)$$

where t_0 is moment of contact separation, C and D are constants.

The values of the constants for three typical $\frac{di}{dt}$ characteristics are given by Table 4.2 as given in [14].

Table 4.2 Constants for equation (4.3) (Reproduced from [14]).

$\frac{di}{dt}$ TYPE	C(A/MS ²)	D(A/ MS)
High	-0.034	255
Medium	0.31	155
Low	1	190

4.4 Simulation Results

To characterize the various behaviors of the VCB model discussed and validate them, the test circuit in Fig.3 based on [16] is used. To this end, the effects of arcing time, rate of rise of dielectric strength, high frequency current quenching capability, and prestrikes have been considered. Total unsuccessful operation of the breaker where it is unable to interrupt all current zeros and successful interruption at high frequency current zero are also demonstrated.

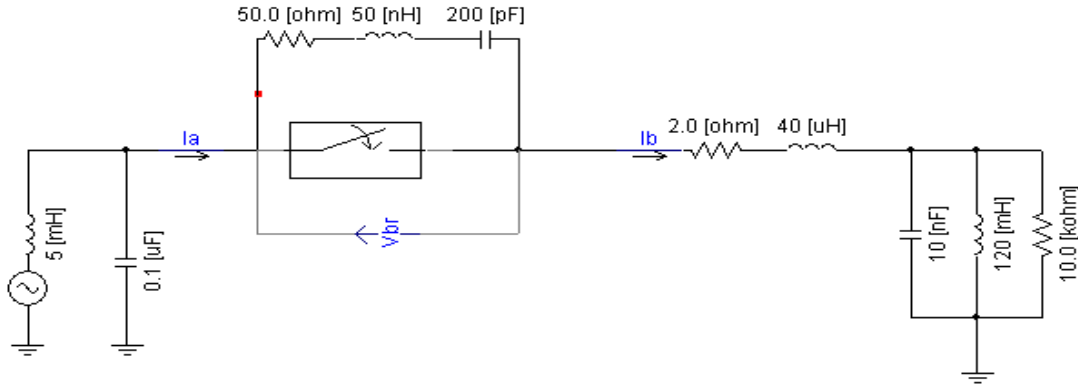


Fig. 4.3 Test Circuit.

4.4.1 Effect of Arcing Time

Arcing time is defined as the time between the initiation of breaker opening to the next power frequency current zero. In the first case, the breaker is opened at $t_0 = 0.104$ s and the next current zero of the power frequency current comes at $t = 0.105$ s. This gives an arcing time of $AT = 1$ ms. *Fig. 4.4* (left) shows the resulting breaker voltage and current for this case. The breaker can not break the arc successfully at the first current zero and successful interruption occurs at the second current zero when the breaker has developed enough with stand voltage at a bigger gap distance. *Fig. 4.4* (right) shows breaker voltage and current for a larger arcing time of $AT = 5$ ms, all other parameters remaining the same. For this case the breaker is opened at $t_0 = 0.1$ sec., 4ms earlier and the breaker has developed enough gap withstand voltage by the time of the first current zero and thus it is able to interrupt the arc successfully at this current zero.

The higher the arcing time, the longer the time the breaker gets to develop a bigger and sufficient dielectric strength to break the arc.

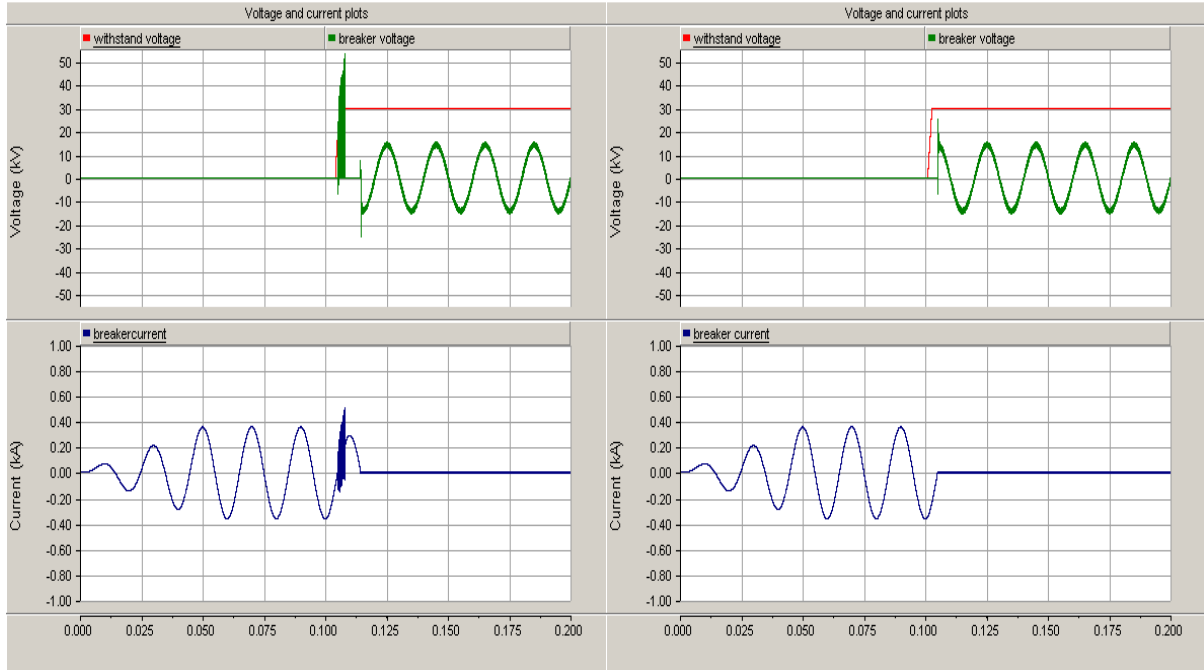


Fig.4.4 Unsuccessful (left) and successful (right) interruptions at first current zero for arcing times of 1ms and 5ms respectively.

4.4.2 Effect of rate of rise of dielectric strength

The rate of rise/fall of the dielectric strength depends on how fast the breaker contacts are opening or closing respectively. All other parameters remaining constant, if the rate of rise is increased, the breaker reaches a higher dielectric strength faster and the probability that the breaker quenches the arc at first power frequency current zero increases. This has been demonstrated in *Fig. 4.5*(left) which shows breaker voltage and current for a rate of rise of $A=4.7\text{kV}/\mu\text{s}$ in which case there is unsuccessful interruption of arc at the first current zero. A successful interruption occurs at the following power frequency zero. Now, if the rate of rise is increased to $A=17\text{kV}/\mu\text{s}$ as shown in *Fig.4.5* (right), the breaker has successfully interrupted the arc at the first current zero.

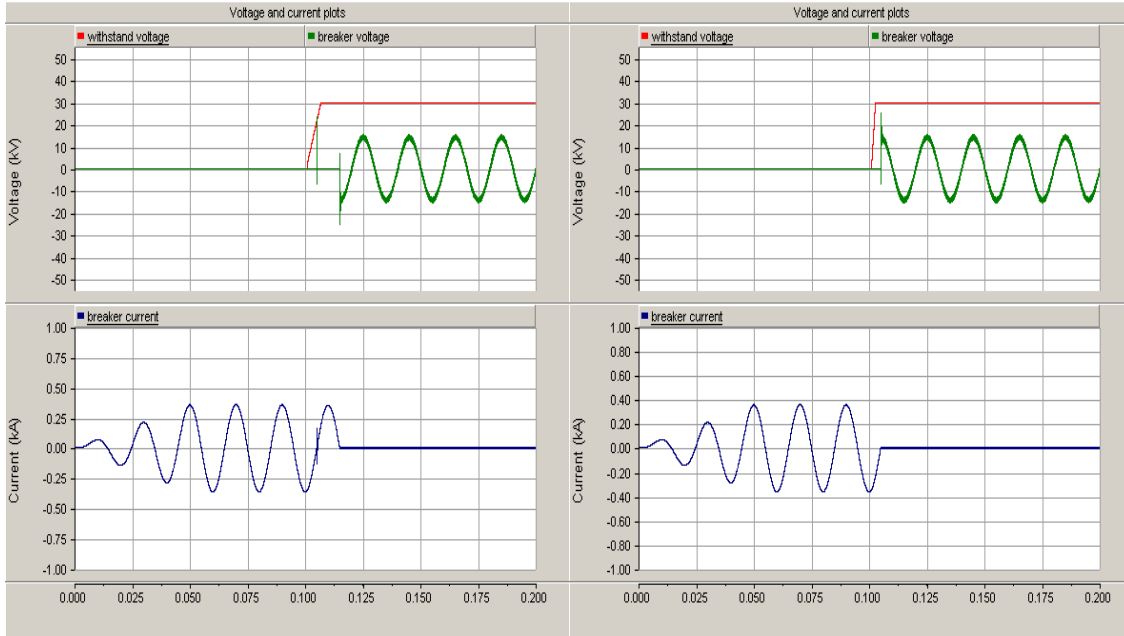


Fig.4.5 Unsuccessful (left) and successful (right) interruptions at first current zero for RRDS $A=4.7\text{kV}/\mu\text{s}$, and $A=17\text{kV}/\mu\text{s}$ respectively.

4.4.3 Effect of high frequency quenching capability

The variation of quenching capability has been considered in this case by taking the high and medium quenching capabilities keeping all other parameters the same for both cases. As it is shown in Fig.4.6 and Fig.4.7, the higher the quenching capability, the larger the number of reignitions will be. This is because of the high transient recovery voltage across the breaker when interrupting currents with high $\frac{di}{dt}$. This is also clearly shown in the zoomed plots of Fig.4.6 and Fig.4.7 for the two cases. On the other hand, if the quenching capability is smaller, the current may not be chopped during the high frequency period, this leads to an increase in conduction period of the high frequency component (smaller number of re-ignitions). The latter case might cause failure of interruption.

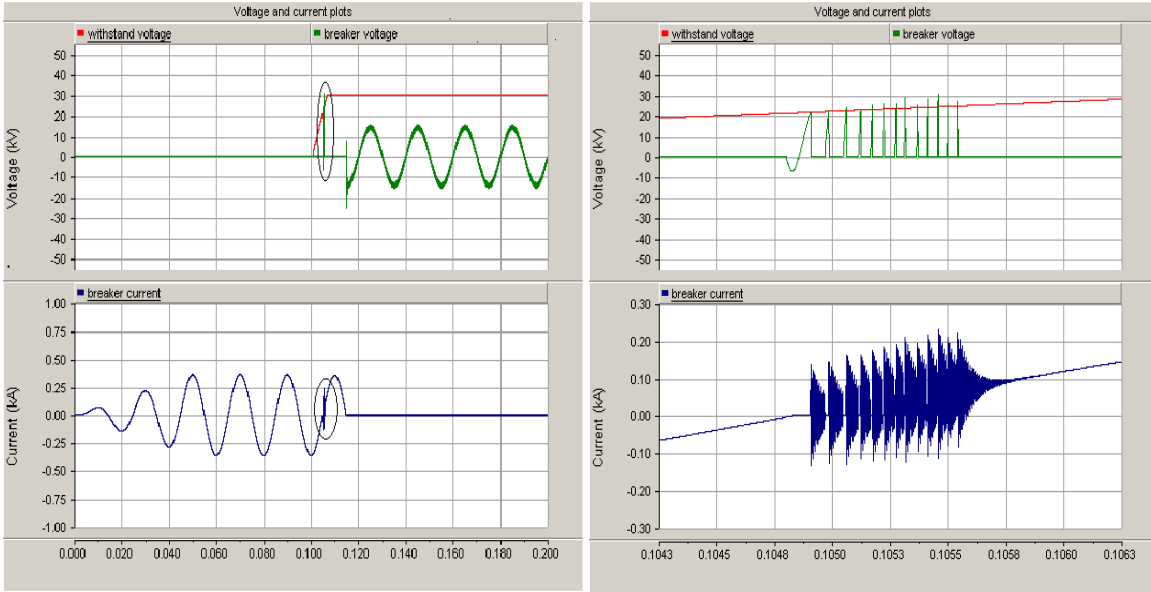


Fig.4.6 Plots showing the effect of high frequency quenching capability for arcing time of 5ms and high $\frac{di}{dt}$ type.

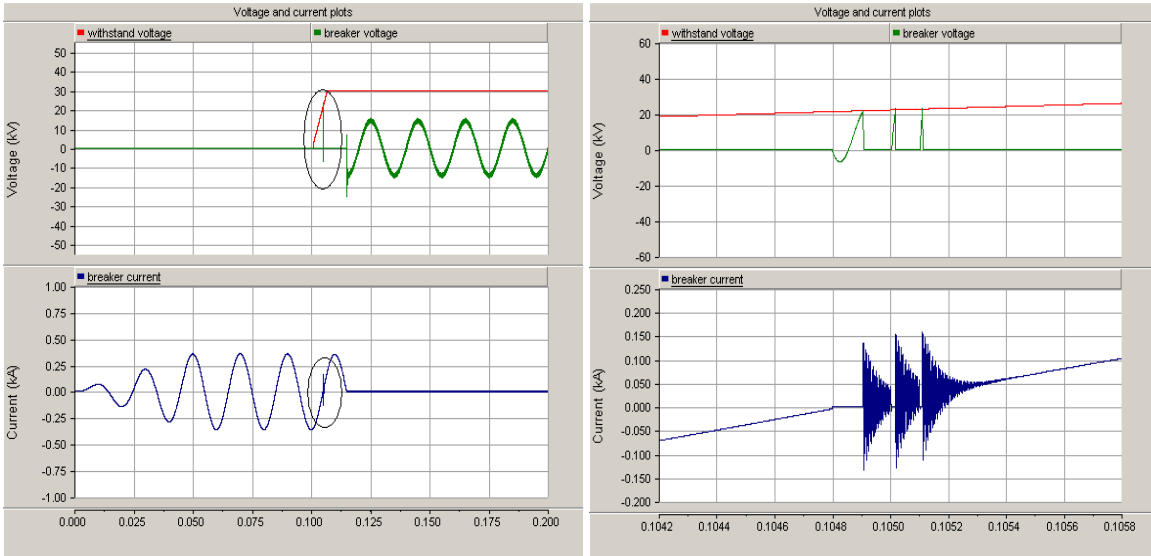


Fig.4.7 Plots showing the effect of high frequency quenching capability for arcing time of 0.005 and medium $\frac{di}{dt}$ type.

4.4.4 Breaker unsuccessful and high frequency current successful operation

When a vacuum circuit breaker reignites during opening operation, voltage escalation occurs and interruption process can terminate in one of the three cases [19].

- a. The breaker fails to interrupt the high frequency current, and interruption is accomplished in one of the next power frequency zeros.
- b. The breaker fails to interrupt and may cause harm to itself and/or the equipments connected to.
- c. The breaker can successfully interrupt at one of the high frequency current zeros.

The first case is shown in Figures (4.4, 4.5, 4.6 and 4.7). Case two and three are illustrated in *Fig.4.8* and *Fig.4.9*. Transition from case two to three was achieved by increasing the breakdown voltage when the breaker is fully open from 20kV in case two to 26kV in three.

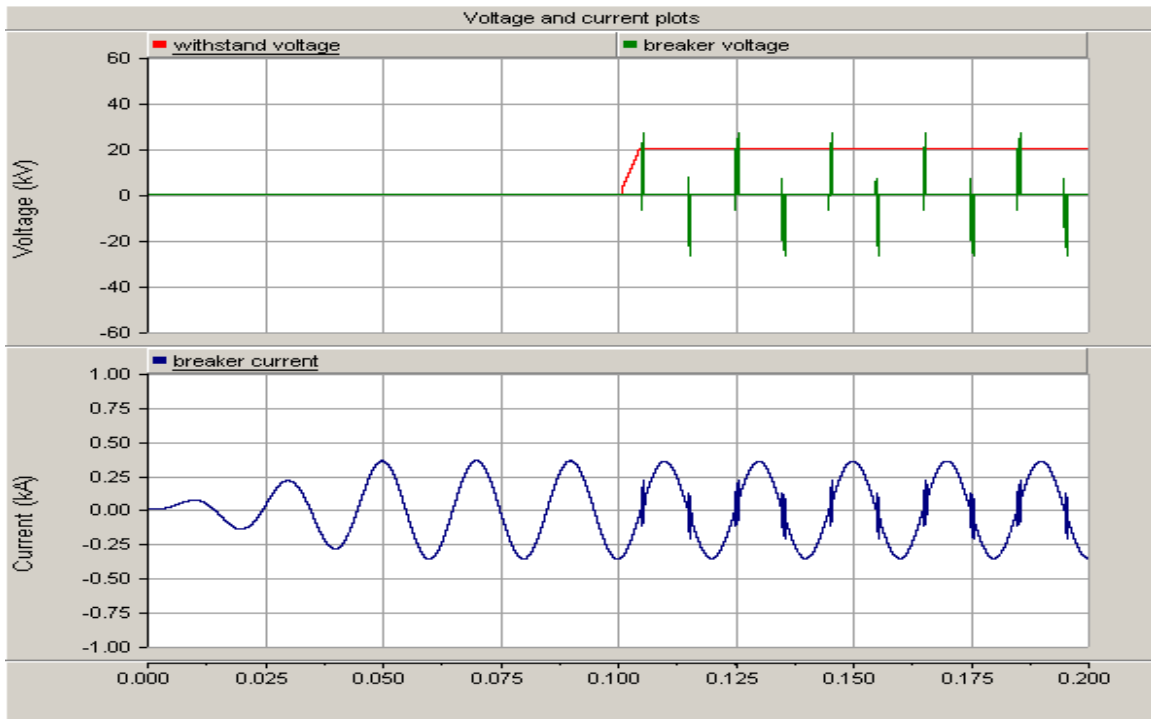


Fig.4.8 Unsuccessful breaker operation.

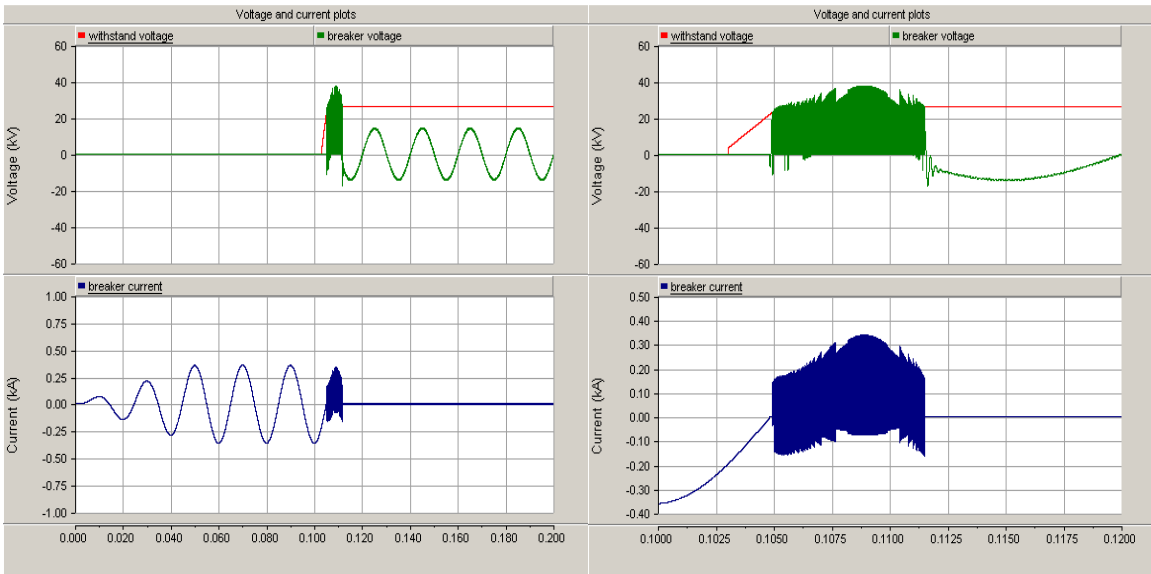


Fig4.9 Successful interruption of high frequency current.

4.4.5 Pre-strikes

During closing operation of a vacuum circuit breaker, due to the diminishing dielectric strength of the gap as the contact separation decreases, the gap may break and an arc is established before real galvanic contact occurs. For the same reasons as for re-ignition, during opening operation, a number of pre-strikes can happen in the gap during closing. The effect of pre strikes is illustrated in *Fig.4.10*, where very steep breaker step voltages are shown to have developed, due to the high frequency current quenching.

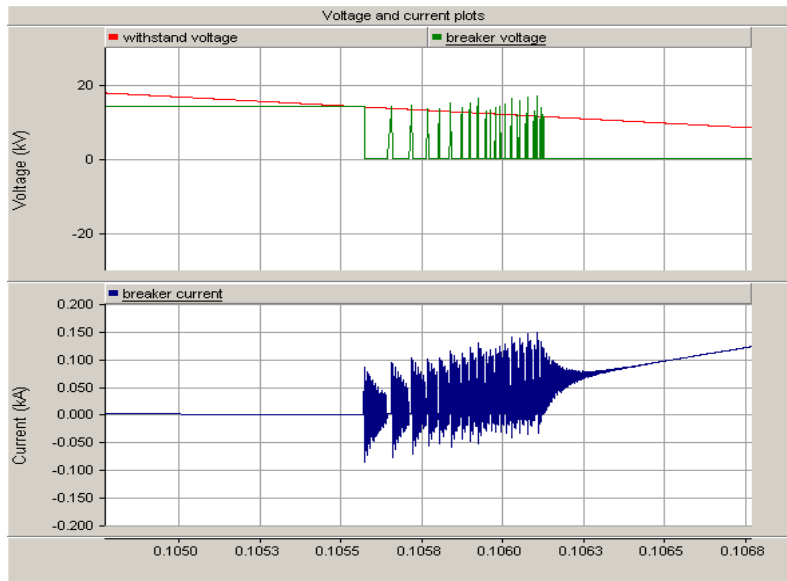


Fig.4.10 Pre strike during contact closing.

4.5 Conclusions

- ✚ Interruption of small but non zero power frequency inductive currents and subsequent high frequency currents due to re ignitions and pre-strikes by VCBs causes generation of very steep TOVs.
- ✚ A statistical model of the VCB based on modeling of current chopping, dielectric strength and high frequency current quenching capability was used in a generic test circuit to characterize properties of an actual VCB and expected results were found.

Chapter 5

TRANSFORMER MODELING -Background and Theory

5.1 Introduction

In the previous sections it was shown that the transients caused by the switching action of the VCB have a wide range of frequencies. During the prestrike and restrike of a VCB for example high-frequency oscillations with short rise time are produced. Consequently the transformer model proposed in this work should adequately represent the transformer over a wide range of frequencies from 50/60Hz to MHz. However, the transformer representation used in PSCADE/EMTDC does not take into account the high frequency behavior of the transformer like the other devices modeled in previous sections. Many papers have tried to deal with this problem. A model to simulate the high frequency behavior of a power transformer is presented in [22], and [23].

A number of high frequency transformer models have been proposed by different authors. Internal winding models and terminal models are the two broad categories.

Internal winding models

Very fast TOVs voltages can generate a voltage oscillation inside the transformer windings. Current chopping and reignition of a VCB give rise to fast electromagnetic transients in power networks, which may result in high frequency oscillations and overvoltage stresses on the terminals of network components. The effects of such transients on transformer windings are particularly important. Most of the time, the greatest problem is the internal resonance which occurs when the frequency of the input surge is equal to some of the resonance frequencies of the transformer. These overvoltages are characterized by a very short rise time. Most of the time, resonant overvoltages can cause a flashover from the windings to the core or between the turns. The inter- turn insulation is particularly vulnerable to high-frequency oscillation, and therefore, the study of the distribution of inter-turn overvoltages is of essential interest [21].

The internal winding model is generally applicable if calculating inter-turn voltages in windings of the transformer during transient conditions are of interest in the study. Besides at the design stage, an accurate calculation of overvoltages which would stress winding sections is very important for economical use of the insulation material. On the other hand, in HV and EHV networks, prediction of possible voltage stresses at critical points is required for efficient insulation coordination and protection. These models

assumed that the winding configuration, geometry, material constants and other construction details are known.

Terminal models

In the majority of problems related to power system transients, transformers are considered as system components. Transformer terminal models are based on the simulation of the frequency and/or time domain characteristics at the terminals of the transformer. A number of studies dealing with modelling of the power system equipment based on terminal measurements have been published, example [22], [23]. External measurements can be performed either in the frequency or time domain. Frequency domain data consist of terminal impedance or admittance characteristics, whereas time domain data is basically acquired from impulse voltage tests.

The model proposed in this thesis belongs to terminal model as the interest is on the transient over voltages at the terminals associated due to interaction of the different components in the system, for example switching operation of the VCB.

5.2 Wide Band Modelling of Power Transformers

The high-frequency behaviour of power transformers is characterized by several resonance points due to inductive and capacitive effects from the windings, tank, and core. This behaviour should be included in any overvoltage study where the high-frequency characteristics of the transformer is of significance (e.g., transferred over voltages and resonant over voltages)[23].

In this thesis a method for the development of a wide band frequency dependent black box model of a transformer is provided.

This model is based on experimental determination of the admittance matrix in a wide frequency range and subjecting the measured admittance matrix to an approximation with a rational function by the method of vector fitting. The rational function so obtained can then be realized in to an RLC net work for time domain simulation in PSCAD/EMTDC.

The following sections are devoted to describing the modelling techniques used to obtain the model.

5.2.1 Measurements

Consider a transformer with n –terminals as shown in *Fig5.1*. The voltage and current at the terminals can be expressed as

$$I(s) = Y(s)V(s) \quad (5.1)$$

where $Y(s)$ is the admittance matrix, $V(s)$ is terminal voltage vector and $I(s)$ is terminal current vector all in frequency domain. $Y(s)$ is an n by n symmetrical matrix while $I(s)$ and $V(s)$ are vectors of length n .

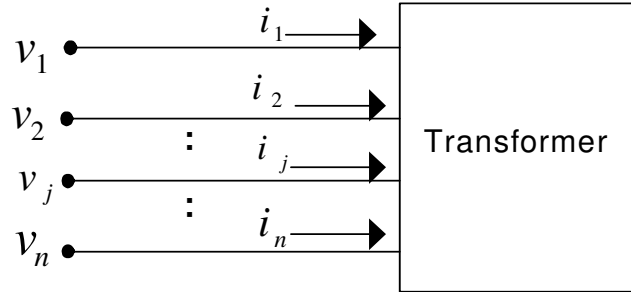


Fig. 5.1 N -terminal Transformer Model.

(5.1) can be expanded as

$$\begin{bmatrix} I_1 \\ I_2 \\ \cdot \\ \cdot \\ \cdot \\ I_n \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} & \dots & Y_{1n} \\ Y_{21} & Y_{22} & \dots & Y_{2n} \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ \cdot & \cdot & & \cdot \\ Y_{n1} & Y_{n2} & \dots & Y_{nn} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ \cdot \\ \cdot \\ \cdot \\ V_n \end{bmatrix} \quad (5.2)$$

It can be seen from (5.1) that applying a voltage V_j to terminal j and zero voltage to the remaining terminal will produce the j^{th} column of $Y(S)$, where the element Y_{ij} can be found by taking the ratio I_i to V_j . This is demonstrated for the first column of $Y(S)$.

Apply V_1 to terminal 1 and short circuit all other terminals, (5.2) can be reduced to

$$I_1 = Y_{11}V_1 \quad (5.3)$$

$$I_2 = Y_{21}V_1 \quad (5.4)$$

\cdot

\cdot

\cdot

$$I_n = Y_{n1}V_1 \quad (5.5)$$

From (5.3), (5.4) and (5.5)

$$Y_{11} = \frac{I_1}{V_1}, Y_{21} = \frac{I_2}{V_1}, Y_{i1} = \frac{I_i}{V_1}, Y_{n1} = \frac{I_n}{V_1} \quad (5.6)$$

The same procedure can be used to find all the columns of Y. In general the procedure used to measure the admittance is depicted in Fig.5.2.

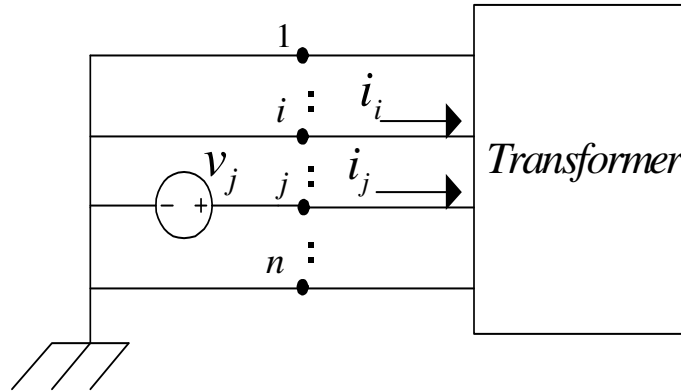


Fig.5.2 Measuring element of the j^{th} column of Y ($Y_{ij} = \frac{I_i}{V_j}, Y_{jj} = \frac{I_j}{V_j}$).

The measurements were performed on three test transformer. A single phase transformer at Chalmers University of Technology and two three phase transformers at ABB Corporate Research.

In both the three phase transformers, the high voltage winding are connected in delta and the low voltage windings are connected in wye.

The admittance matrix for the test transformers has been measured using the measuring technique outlined in Fig.5.2. This matrix has a size of 2x2 and 6x6 for the single and three phase test transformers respectively; hence (5.7) in its simplified form for the single and three phase test transformers can be re written by (5.8) and (5.9). The terminal identification in these equations is according to Fig.5.3.

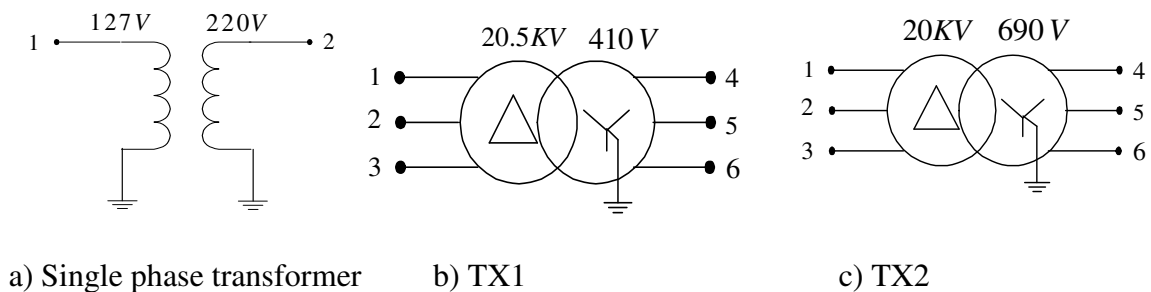


Fig.5.3 Test transformers.

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} \quad (5.7)$$

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ I_4 \\ I_5 \\ I_6 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} & Y_{13} & Y_{14} & Y_{15} & Y_{16} \\ Y_{21} & Y_{22} & Y_{23} & Y_{24} & Y_{25} & Y_{26} \\ Y_{31} & Y_{32} & Y_{33} & Y_{34} & Y_{35} & Y_{36} \\ Y_{41} & Y_{42} & Y_{43} & Y_{44} & Y_{45} & Y_{46} \\ Y_{51} & Y_{52} & Y_{53} & Y_{54} & Y_{55} & Y_{56} \\ Y_{61} & Y_{62} & Y_{63} & Y_{64} & Y_{65} & Y_{66} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_3 \\ V_3 \\ V_6 \end{bmatrix} \quad (5.8)$$

Consider the situation that the transformer terminals are divided into two groups, denoted by H and L, to represent the High voltage and Low voltage terminals respectively. This partitioning of the terminal or winding simplifies the problem. (5.7) and (5.8) can then be written in the form

$$\begin{bmatrix} I_L \\ I_H \end{bmatrix} = \begin{bmatrix} Y_{LL} & Y_{LH} \\ Y_{HL} & Y_{HH} \end{bmatrix} \begin{bmatrix} V_L \\ V_H \end{bmatrix} \quad (5.9)$$

$$\begin{bmatrix} I_H \\ I_L \end{bmatrix} = \begin{bmatrix} Y_{HH} & Y_{HL} \\ Y_{LH} & Y_{LL} \end{bmatrix} \begin{bmatrix} V_H \\ V_L \end{bmatrix} \quad (5.10)$$

Where I_L, V_L and I_H, V_H are the current and voltage at the low and high voltage terminals and the Sub matrixes $Y_{HH}, Y_{HL}, Y_{LH}, Y_{LL}$ are of size 1x1 and 3x3 for the single and three phase transformer respectively as it can be seen from (5.7) and (5.8) .

It is also interesting to mention the symmetry of the sub matrix. This is due to the symmetry of the windings.

If the high voltage (H) terminals are open-circuited, we can easily get the voltage ratio from high to low by putting $I_H = 0$ in (5.9) and (5.10).

$$V_{HL} = \frac{V_H}{V_L} = -Y^{-1}_{HH} Y_{HL} , \text{ for } I_H = 0 \quad (5.11)$$

Similarly if the low voltage (L) terminals are open-circuited the voltage ratio from low to high can be obtained by setting $I_L = 0$ in (5.9) and (5.10).

$$V_{LH} = \frac{V_L}{V_H} = -Y^{-1}_{LL} Y_{LH} , \text{ for } I_L = 0 \quad (5.12)$$

It can be easily noted from (5.11) and (5.12) V_{HL} , V_{LH} are matrices of size 1 by 1 and 3 by 3 for a single phase and three phase transformer respectively.

The voltage ratios from Low to High and from High to Low can be measured using the set up given in Fig.5.4 and Fig.5.5 which demonstrates this clearly.

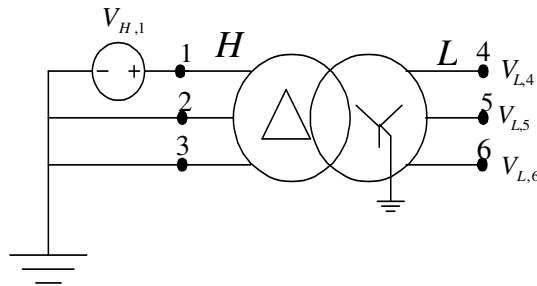


Fig.5.4 Measurement of the first column of

$$V_{LH} (V_{LH,41} = \frac{V_{L,4}}{V_{H,1}}, V_{LH,51} = \frac{V_{L,5}}{V_{H,1}}, V_{LH,61} = \frac{V_{L,6}}{V_{H,1}}).$$

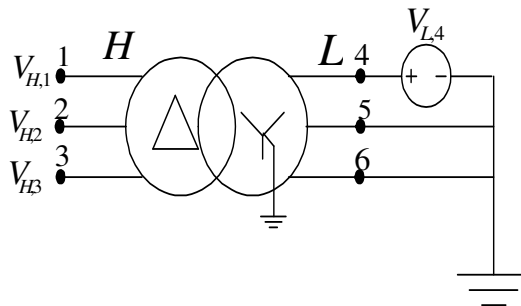


Fig.5.5 Measuring element of the first column of

$$V_{HL} (V_{HL14} = \frac{V_{H,1}}{V_{L,4}}, V_{HL24} = \frac{V_{H,2}}{V_{L,4}}, V_{HL34} = \frac{V_{H,3}}{V_{L,4}}).$$

5.2.2 Rational Approximation of Frequency Responses by Vector Fitting

This section briefly reviews the method of rational approximation by vector fitting. The method is used for the fitting of measured or calculated frequency domain responses into a rational function that approximates the response very well. It can be employed both for single as well as for several frequency responses of a system. The method was developed by Björn Gustavsen et al based on reformulation of the Sanathanan–Koerner iteration and has been found to be very suitable for fitting network equivalents and transformer responses. Some examples where this method can be used are:

- Network equivalent for portion of a large network

- High-frequency transformer model based on measured frequency responses
- Transfer of voltages from transformer terminals to internal points in winding
- Transmission line modeling

The method is later applied to fit the admittance matrix of power transformers in coming sections.

The Vector Fitting Algorithm

Generally speaking, an approximation of a given order can be obtained by fitting a given set of frequency dependent data to a ratio of polynomials as shown in below [27].

$$f(s) \approx \frac{a_0 + a_1s + a_2s^2 + a_3s^3 + \dots + a_Ns^N}{b_0 + b_1s + b_2s^2 + b_3s^3 + \dots + b_Ns^N} \quad (5.13)$$

To write this non linear equation as a linear problem of the type $Ax=b$ with the coefficients as unknowns, both sides should be multiplied with the denominator. This, however, produces a badly scaled and ill-conditioned problem as the columns of A are multiplied with different powers of s . This imposes a limitation on the applicability of the approximation to very lower order only. A more efficient method is therefore required. Of the many fitting algorithms developed to date, Vector fitting has been found to be very efficient to model transformer responses and network equivalents.

The idea of vector fitting is to find a rational function approximation which is sum of partial fractions from the given frequency response data. This is done by replacing a set of starting poles with an improved set of poles via an iterative pole relocation method based on least squares approximation of linear problems [27]. The starting poles are so chosen to cover the frequency range of interest and should be linearly or logarithmically distributed over the whole range. It is recommended to choose complex conjugate pole pairs for functions with distinct resonance peaks like transformer responses as starting poles. For smooth functions real poles are sufficient.

To demonstrate the method of vector fitting, consider the rational function approximation

$$f(s) = \sum_{n=1}^N \frac{c_n}{s - a_n} + d + s.e \quad (5.14)$$

where $f(s)$ is a frequency dependent transfer function of a single response or a matrix of several responses, c_n and a_n are the residues and poles respectively which can be real or conjugate pairs and d and e are real. N is the order of approximation. The intention is to approximate the response $f(s)$ by the terms on the right hand side of the equation. This requires computation of the unknowns- c_n , a_n , d and e . An approximation of $f(s)$ in a given frequency range is therefore achieved this way. Since one of the unknowns a_n in (5.14) is in the denominator, the problem is a non linear one. Therefore, the problem should be linearized before it is solved. The algorithm of vector fitting tackles the

problem in two steps. In the first step, the poles are identified and in the second step residues are identified.

1. Step 1

Here, a set of starting poles \bar{a}_n are chosen for $f(s)$ and (5.14) is multiplied by an unknown function $\sigma(s)$ which is also approximated with a rational function with the same starting poles.

$$\sigma(s) \approx \sum_{n=1}^N \frac{\tilde{c}_n}{s - \bar{a}_n} + 1 \quad (5.15)$$

An augmented problem can thus be written

$$\begin{bmatrix} f(s) \sigma(s) \\ \sigma(s) \end{bmatrix} \approx \begin{bmatrix} \sum_{n=1}^N \frac{c_n}{s - \bar{a}_n} + d + s.e \\ \sum_{n=1}^N \frac{\tilde{c}_n}{s - \bar{a}_n} + 1 \end{bmatrix} \quad (5.16)$$

To have a linear problem in the unknowns c_n , \tilde{c}_n , d and e , the second row of (5.16) is multiplied by $f(s)$ giving

$$\sum_{n=1}^N \frac{c_n}{s - \bar{a}_n} + d + s.e \approx \left(\sum_{n=1}^N \frac{\tilde{c}_n}{s - \bar{a}_n} + 1 \right) f(s) \quad (5.17)$$

$$(\sigma f)_{fit}(s) = \sigma_{fit}(s) f(s) \quad (5.18)$$

is a linear problem of the type $Ax=b$ in the frequency range of interest with the above stated unknowns in the solution vector x . For a given frequency S_k

$$A_k x = b_k \quad (5.19)$$

where $A_k = \left[\begin{array}{ccccccc} \frac{1}{s_k - \bar{a}_1} & \dots & \frac{1}{s_k - \bar{a}_2} & 1 & s_k & \frac{-f(s_k)}{s_k - \bar{a}_1} & \dots & \frac{-f(s_k)}{s_k - \bar{a}_1} \end{array} \right]$ (5.20)

$$x = [c_1 \dots c_N \quad d \quad e \quad \tilde{c}_1 \dots \tilde{c}_n]^T \quad (5.21)$$

$$b_k = f(s_k) \quad (5.22)$$

From (5.18), we have

$$f(s) = \frac{(\sigma^f)_{fit}(s)}{\sigma_{fit}(s)} \quad (5.23)$$

Since both numerator and denominator of (5.23) have the same poles($s - \bar{a}_n$), the ratio in (5.23) can be rewritten as single fraction instead of sum of partial fractions

$$f(s) = e \frac{\prod_{n=1}^{N+1} s - z_n}{\prod_{n=1}^N s - \tilde{z}_n} \quad (5.24)$$

It is clearly seen from (5.24) that the zeros of $\sigma_{fit}(s)$ are equal to the poles of $f(s)$. Thus by calculating the zeroes from the linear equation of (5.15), a good set of poles for the fitted $f(s)$ is obtained.

2. Step 2

Now the identification of the residues of the function $f(s)$ remains in order to have a complete fit of its rational approximation. If the zeroes of $\sigma_{fit}(s)$ calculated in step 1 are used in the original problem in (5.14) as new poles, we thus have a linear problem where the residues can be easily solved giving the unknowns c_n , d and e .

For more complete and deeper treatment of how the vector fitting algorithm is formulated, the reader is referred to [27].

Passivity enforcement

The objective of the rational approximation of the frequency dependent response $f(s)$ in (5.14) using the vector fitting algorithm is to have an equivalent model in the form of a realized network of passive elements when $f(s)$ is an admittance or an impedance function, $Y(s)$ or $Z(s)$. The equivalent model thus obtained is linear, hence the term Passive Linear Time invariant component. If this component is to be included in a transient time domain simulation, it should behave a passive nature in that it should only absorb active power for any set of applied voltages and not produce.

Time domain simulations involving a fitted admittance or impedance may sometimes lead to an unstable time domain simulation due to non passivity. There are also cases where the model could be stable and still non passive in which case unstable simulations arise when the model is used in an interconnection with other components. It is, therefore, important to check that the equivalent network contains no passivity violations over the whole frequency range and outside the frequency range as well. If violations exist, they should be removed. This procedure of removing passivity violations is termed Passivity Enforcement.

A requirement for the fitted admittance $Y(s)$ to be passive is for the real part of the admittance to be Positive Definite, which means all eigenvalues of G should be real positive. A general procedure to enforce passivity to the network is to calculate a correction for the approximated rational function so that it becomes Positive Definite [28]. This corrective perturbation should be as minimal as possible since it causes a fitting error of the actual data. One way to achieve minimum correction is to have very accurate measurement of the response. A formal formulation of the PD criterion is given below [28].

Passivity Criterion

Consider a component defined by an admittance matrix $Y(s)$ in the frequency domain

$$I=Y v \quad (5.25)$$

where I and v are current and voltage complex vectors. The absorbed power is therefore given as

$$P=\text{Re} \{v^*Y v\} =\text{Re} \{v^*(G+jB)v\}=\text{Re} \{v^*Gv\} \quad (5.26)$$

where $*$ means transpose of conjugate of v .

It follows from (5.26) that the real power P will always be positive if all eigenvalues of G are positive, entailing the PD criterion.

For further and detailed reading on passivity enforcement the reader is referred to [29].

5.2.3 Time Domain Implementation

The basic idea behind the new transformer model is to produce an equivalent network whose admittance matrix matches the admittance matrix of the original transformer over the frequency range of interest. The next question is how we get this equivalent network. This equivalent network can be obtained by realization of the fitted admittance matrix $Y_{fit}(s)$.

The procedure to obtain the network equivalent is given in the APPENDIX and summarized here. Consider the admittance matrix Y of a transformer obtained using the measurement procedure in section 5.2.1 and fitted with a rational function using the VF method given in section 5.2.2 creating a matrix $Y_{fit}(s)$ in which the elements are

$$Y_{fit}(s)_{ij} = \sum_{m=1}^N \frac{r_{mij}}{s - a_m} + d_{ij} + s.e_{ij} \quad (5.27)$$

The network has branches between all nodes and ground and between all nodes. Branches between node and ground are given by:

$$y_{ii} = \sum_{j=1}^n Y_{fit}(s)_{ij} \quad (5.28)$$

while the branches between node i and node j are

$$y_{ij} = -Y_{fit}(s)_{ij} \quad (5.29)$$

where n is the size of the matrix which is 2 for single and 6 for the three phase transformers.

Consider now a single branch $y(s)$ of the network (node to ground or between two nodes) fitted with real and complex conjugate poles

$$y(s) = \frac{r_1}{s-a_1} + \frac{r_2}{s-a_2} + \dots + \frac{r_1' - jr_1''}{s-(a_1' - ja_1'')} + \frac{r_1' + jr_1''}{s-(a_1' + ja_1'')} + \frac{r_2' - jr_2''}{s-(a_2' - ja_2'')} + \frac{r_2' + jr_2''}{s-(a_2' + ja_2'')} + \dots + d + s.e \quad (5.30)$$

The synthesis of (5.30) is an RLC network of parallel branches as shown in *Fig.5.6*.

where

$$R_0 = \frac{1}{d}, \quad C_0 = e \quad (5.31)$$

The real pole is represented by the RL circuit as

$$L_r = \frac{1}{r}, \quad R_r = \frac{-a}{r} \quad (5.32)$$

while the complex conjugate pair is given by RLCG network, where

$$L_c = \frac{1}{2r'}, \quad R_c = 2L_c(L_c(r'a' + r''a'') - a') \quad (5.33)$$

$$C_c = \frac{1}{L_c(a'^2 + a''^2 + 2R_c(r'a' + r''a''))}, \quad G_c = -2L_c C_c(r'a' + r''a'') \quad (5.34)$$

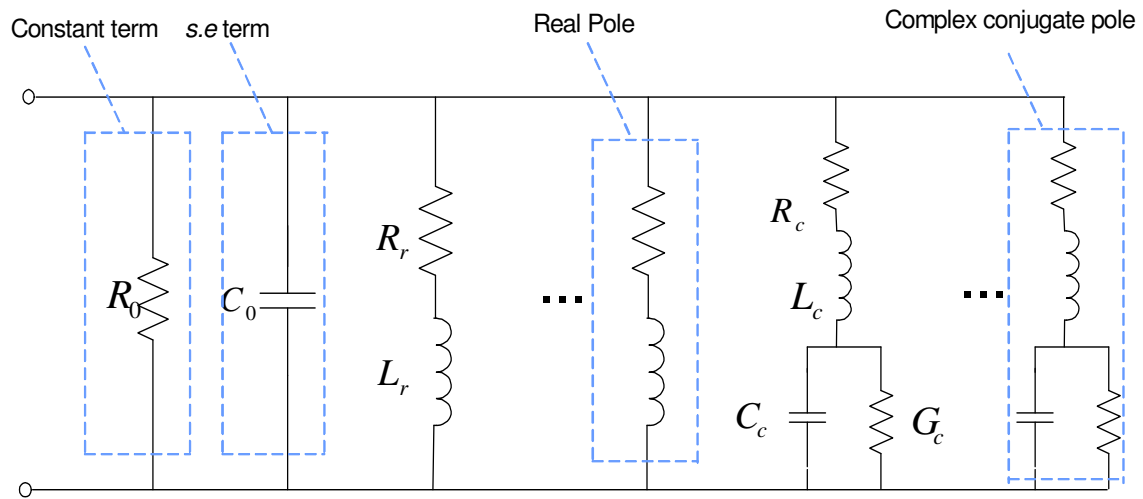


Fig.5.6 Basic structure of the synthesized electrical network for a single element branch.

Chapter 6

TRANSFORMER MODELING-Experiments and Results

6.1 Introduction

In this chapter the measurement setup designed and instrumentations used to measure the admittance matrix and voltage ratio over a wider frequency range is describes in detail .The measurement and fitting result along with their analysis is discussed and finally the model is validated by comparing the measured results with the corresponding calculated and PSCAD/EMTDC simulated results.

6.2 Measurement Setup

The admittance matrix and voltage ratios for the transformers were measured in frequency domain using a network analyzer.The measurement set up as configured to measure one element of the admittance matrix and voltage ratio is outlined in *Fig.5.1* and *Fig.5.2* respectively. The set up consists of the test transformer (a single phase 127/220V and two three phase transformer), the network analyzer to measure the admittance and the voltage ratio over a wide frequency range, current probe for the current measurement and shielded cables which connect the output port of the network analyzer to the transformer terminal for excitation and from the transformer terminal to the input ports of the network analyzer for the purpose of voltage or/and current measurements.

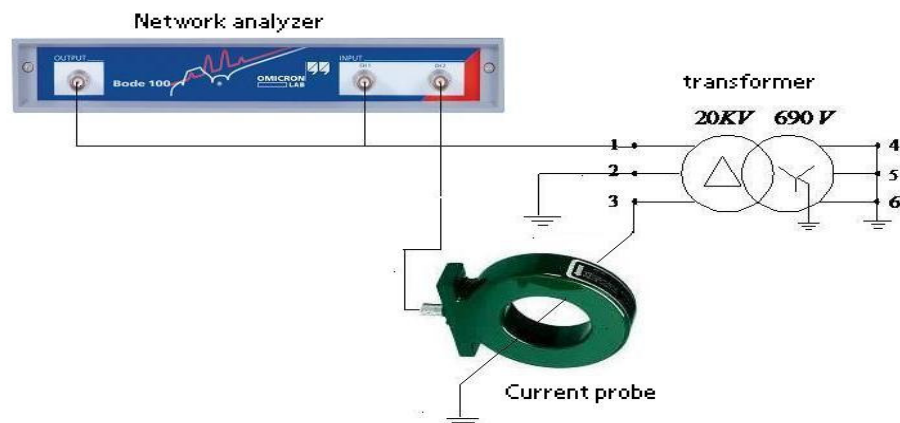


Fig.6.1 Experimental set-up to measure element Y_{31} of the admittance matrix.

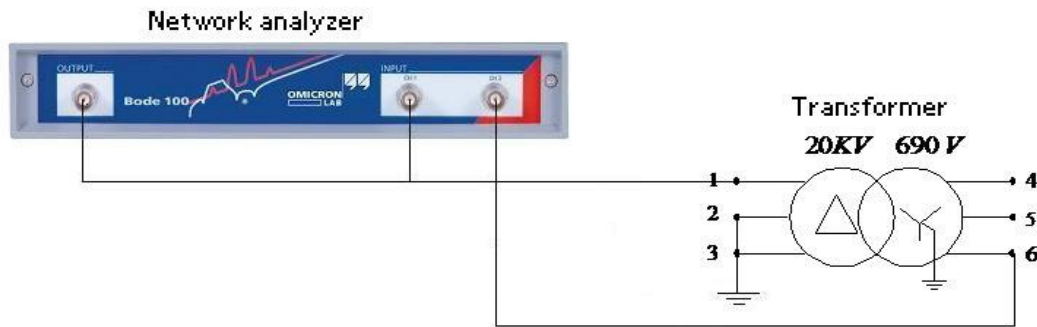


Fig.6.2 Experimental set-up to measure $V_{LH,61} = \frac{V_{L,6}}{V_{H,1}}$ element of the admittance matrix.

Measurement Objects

As it was mentioned earlier the measurements and hence modeling has been done on three transformers but the measurements done on the single phase transformer was an important step to the modeling of two three phase transformers which represent the wind mill (TX1) and the load side transformers of three phase cable systems that has been built at ABB corporate research to emulate a section of an off shore collection wind park model in order to study fast transients that can occur in an off shore wind park.

Windmill Transformer (TX1)

Transformer TX1 (Fig.6.3) in the experimental set up is the representation for one of the windmill transformers in the off shore wind park. It is a 1.25MVA, 410V/20.5kV step up transformer with low voltage side connected in Y and high voltage side in Δ . The transformer data as it is shown in the name plate data is given in Table 6.1.

Load side Transformer (TX2)

The load side transformer TX2 (Fig.6.4) is a 1.0MVA, 690 V/20kV distribution transformer with Δ connected high voltage winding and Y connected low voltage winding. The specification of this transformer is given in Table 6.2.



Fig.6.3 Windmill Transformer (TX1).



Fig.6.4 Load side Transformer (TX2).

Table 6.1 Transformer TX1 data.

NO. 5214242	1999
CTMU 24 HA 1250 (ABB)	IEC 76
1250 kVA Dyn11	50 Hz
20500 ± 2'2.5 % V	35.2 A
410 V	1760 A
U 125AC50/AC8 kV	ONAN
Zk 5.4 %	2885 kg
Pk 11971 W	605 kg
Po 1455 W	

Table 6.2 Transformer TX2 data.

NO. 5210667	1997
CTMU 24 HM 1000	IEC 76
1000 kVA Dyn11	50 Hz
20000 ± 2'2.5 % V	28.87 A
690 V	836.7 A
U 125AC50/AC8 kV	ONAN
Zk 5.1 %	2670 kg
Pk 10260 W	505 kg
Po 1223 W	

Network Analyzer

Two different network analyzers have been used for measurement. This is because the measurements for the single phase transformer were done at Chalmers while for the two three phase transformers they were done at ABB Corporate Research. The MS4630B network analyzer was used to measure the admittance and voltage ratio of the single phase transformer at Chalmers. This network analyzer has a bandwidth of 10Hz to 300MHz, two output (A and B) and three input (R, TA and TB) channels. The Bode 100 network analyzer which was used for the two three-phase transformers measurements has a bandwidth of 10 to 40MHz, one output and two input ports. For both admittance and voltage ratio measurements one output channel which is for the excitation voltage and two input channel; one for voltage and one for current measurement for the case of admittance or both for voltage measurement were required as the admittance and voltage

ratios were measured as the ratio of current to voltage or two voltages, respectively. The specifications of the network analyzers are given in Table 6.3.

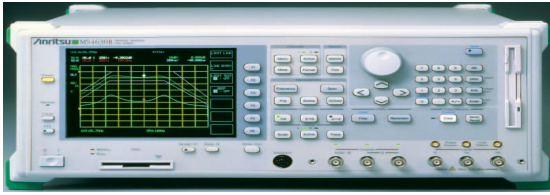


Fig.6.5 MS4630B Network Analyzer.

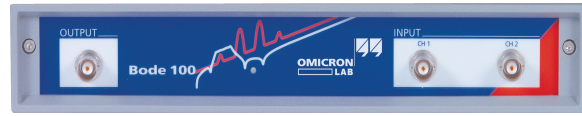


Fig.6.6 Bode 100 Network Analyzer.

Table 6.3 Technical data of the bode 100 network analyzer.

CHARACTERISTIC	MS4630B	BODE 100
Frequency range	10Hz to 300MHz	10 Hz to 40 MHz
Output impedance	50 Ω	50 Ω
Out put Connector	BNC	BNC
Wave form	Sinusoidal signal	Sinusoidal signal
Output voltage	Output A 0 to +21 dBm Output B -6 to +15 dBm	0.01 to 1Vrms into 50 Ω load -27 dBm to 13 dBm
Input Channel	R, TA, TB	CH 1 , CH 2
Input impedance	50 Ω or 1 M Ω	50 Ω or 1 M Ω
Connectors	BNC	BNC
Receiver bandwidth	3, 10, 30, 100, 500 Hz, 1, 2, 3, 4, 5, 10, 20 kHz	10 Hz, 30 Hz, 100 Hz, 300 Hz, 1 kHz, 3 kHz
Sweeping Number of measurement points:	11, 21, 51, 101, 251, 501, 1001	10 to 16501 (freely selectable)

Current Probe

As the admittance elements were measured as the ratio of current to voltage, current probes of model Pearson (Fig.6.7) with sensitivity of 1V/1A for the single-phase transformer and 0.1V/1A for two three-phase transformer measurements has been used.



Fig.6.7 current probes of model Pearson.

6.3 Measurement Results

Fig.6.8 and 6.9 show the magnitudes of the 36 elements of the admittance matrix Y for TX2 and TX1 obtained by direct measurement in four sets of frequency sweeps, two with 801 and 401 sampling points for TX2 and two with 1601 and 801 for TX1. These raw data contain inaccuracies due to noise and other factors as is reflected clearly in the figures. The reproducibility or repeatability of the measurements is, however, indisputably validated in the 4 sets of measurements. The data in Fig. 6.8 a) and 6.8 b) obtained for TX2 are almost the same for the two sets of measurements, with 401 and 801 sampling points respectively. The same is also observed in Fig. 6.9 a) and 6.9b) for TX1, with 801 and 1601 sampling points respectively. The credibility of the data is further enhanced by the large difference in the element sizes which is expected due to the high voltage ratio of the transformers (≈ 50).

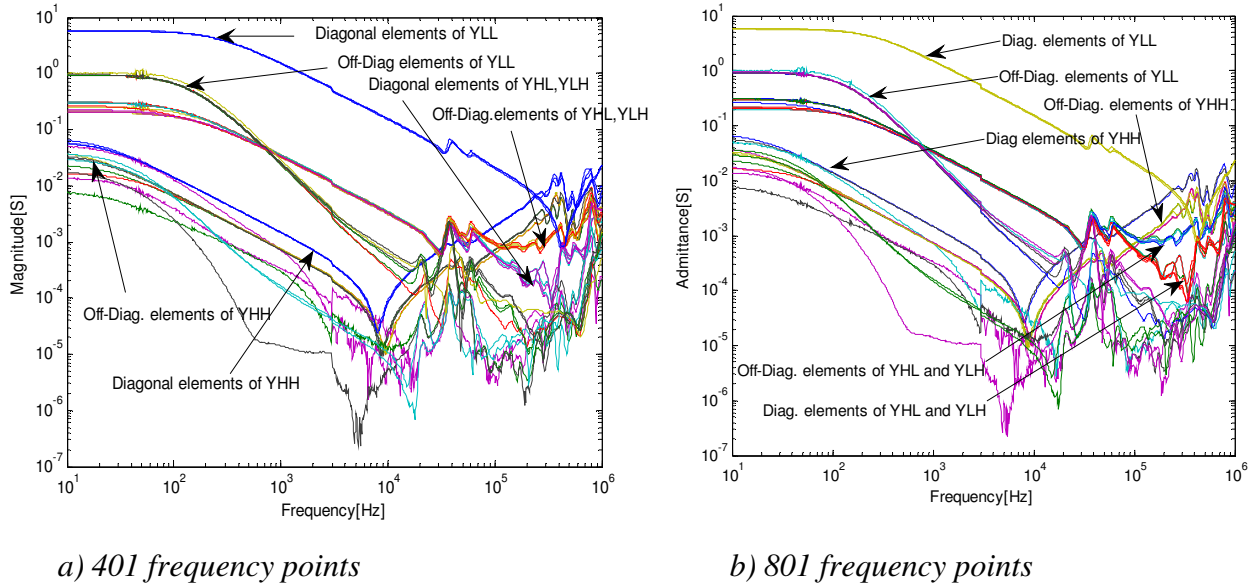
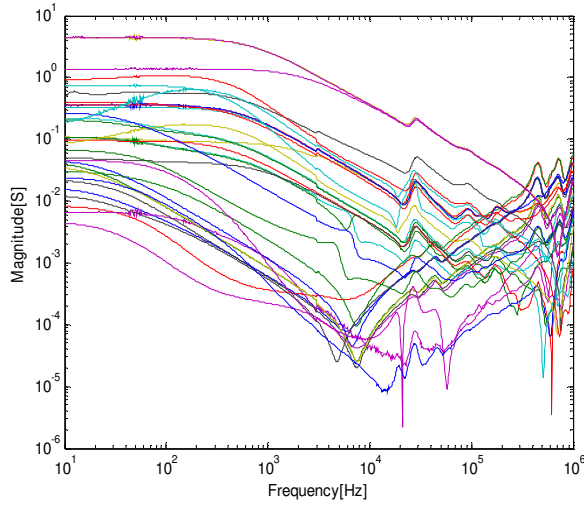


Fig.6.8 Magnitude plot of admittance matrix (raw data) for TX2.

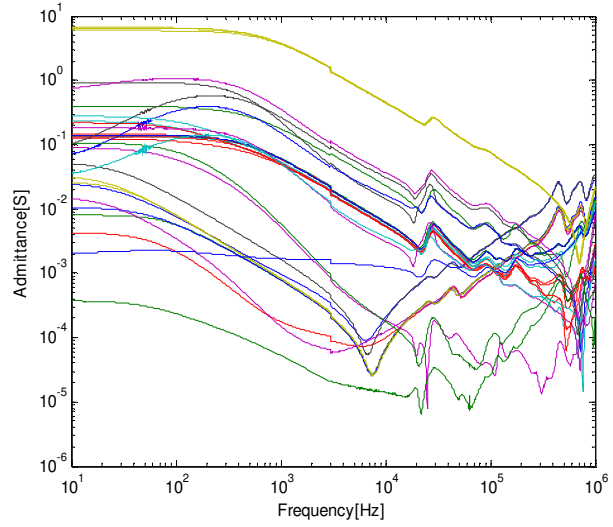
Reproducibility of the data, however, does not always guarantee an accurate data set especially when the cause for the inaccuracy persists. This problem has been tackled by exploiting the symmetry of the transformers and thus of the admittance matrix. Due to this symmetry, several elements of the admittance matrix are identical or closely so. Therefore, bad measurements or noisy measured admittance elements have been replaced with better measured data of another symmetric element. A summary of elements expected to be identical or closely so is given below where Y has been partitioned into four sub matrices as shown in

$$Y = \begin{bmatrix} Y_{HH} & Y_{HL} \\ Y_{LH} & Y_{LL} \end{bmatrix} \quad (6.1)$$

- i) Diagonal elements of Y_{HH}
- ii) Diagonal elements of Y_{LL}
- iii) Diagonal elements of Y_{HL} and Y_{LH}
- iv) Off-diagonal elements of Y_{HH}
- v) Off-diagonal elements of Y_{LL}
- vi) Off-diagonal elements of Y_{HL} and Y_{LH}



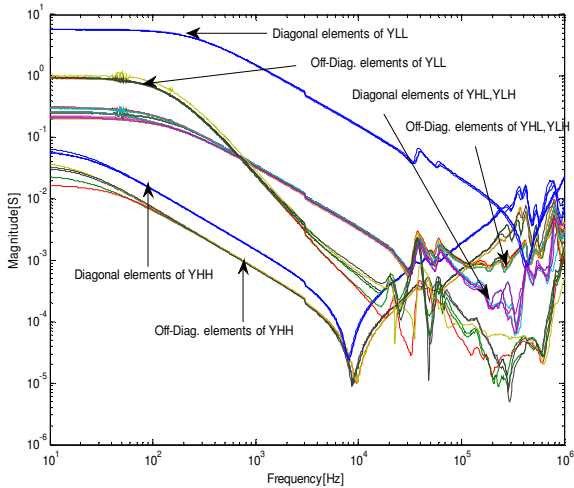
a) 801 frequency points



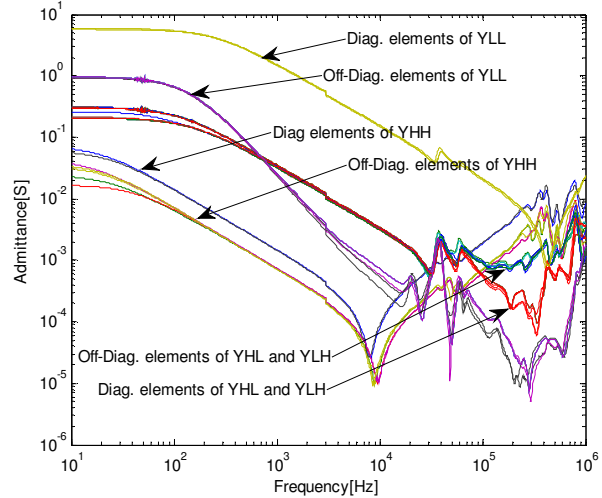
b) 1601 frequency points

Fig.6.9 Measured admittance elements (Raw data) for TX1.

Neater and more accurate data is accordingly found with this modification. The new data set is given in Fig. 6.10 and Fig. 6.11.

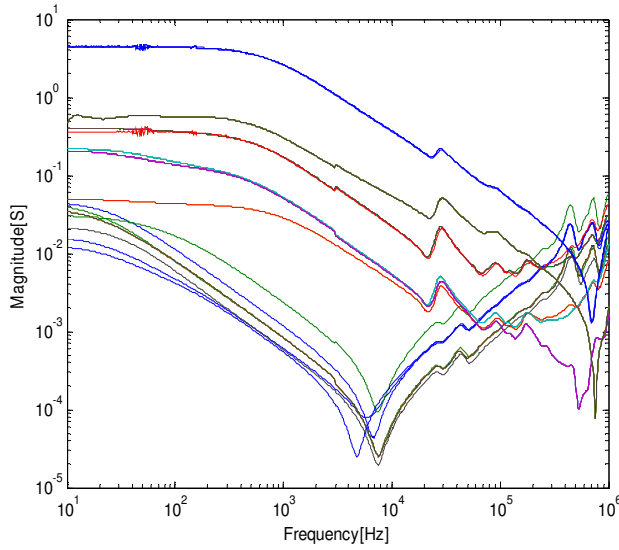


a) 401 frequency points

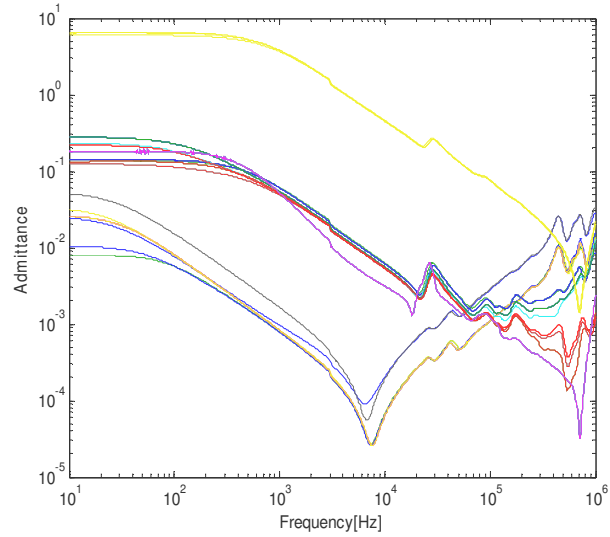


b) 801 frequency points

Fig.6.10 Measured admittance elements modified using symmetry of the sub matrices for TX2.



a) 801 frequency points



b) 1601 frequency points

Fig.6.11 Measured admittance elements modified using symmetry of the sub matrices for TX1.

6.4 Rational Approximation of Admittance Matrices of The Transformers

This section discusses the results of rational approximation of the measured admittance matrices of the power transformers by curve fitting of the frequency response measured at the terminals. The method used is based on a series of papers on curve fitting and open Matlab source codes developed by Björn Gustavsen from SINTEF. Matrix curve fitting is used as the transformer is a multi-terminal device [25]. All the files and Matlab codes on curve fitting can be downloaded from [26].

The frequency-dependent responses are obtained via measurements as discrete functions of frequency. The method applied assumes the transformer as a linear time-invariant and frequency-dependent black box with a certain number of terminals. The frequency response measured is a set of current-voltage ratios over a wide band of frequencies. This gives a three-dimensional admittance matrices of size $n \times n \times N_s$ where n is the number of terminals(nodes) and N_s is the number of measurement points (frequency points). Matrix curve fit is then applied to approximate the elements of the admittance matrix by a rational approximation.

The rational function $f(s)$ given in (5.14) in this case becomes an $n \times n$ admittance matrix as all transformers are multi terminal devices with n terminals. A Matrix curve fit stacks all elements of the matrices into a single column vector $h(s)$ before the elements are fitted.

The curve fitting algorithm was used to approximate all elements of the admittance matrices with a common set of poles. Passivity was also enforced for all elements to ensure stable time simulation.

The original admittance elements are drawn together with their rational approximations for comparison to see how good the fitting is for different orders of approximations. Eigen values of $\text{Re}\{Y\}$ have also been drawn before and after passivity is enforced on all elements for different number and range of frequencies to see the effect of passivity on the error of approximation.

Fig. 6.12 shows the rational approximation of both magnitude and phase of the 36 elements of TX2 with an order of approximation of $N=20$, 3 iterations and passivity over 801 frequency points in the range from 1kHz and 1 MHz. Although the fit in the low frequency segment up to around 10 kHz seems ok, we have a very poor approximation at high frequencies. The total rms-error of approximation in this case is equal to 0.013563. The eigenvalues of $\text{Re}\{Y\}$ before and after passivity enforcement for this case is given in Fig. 6.13.

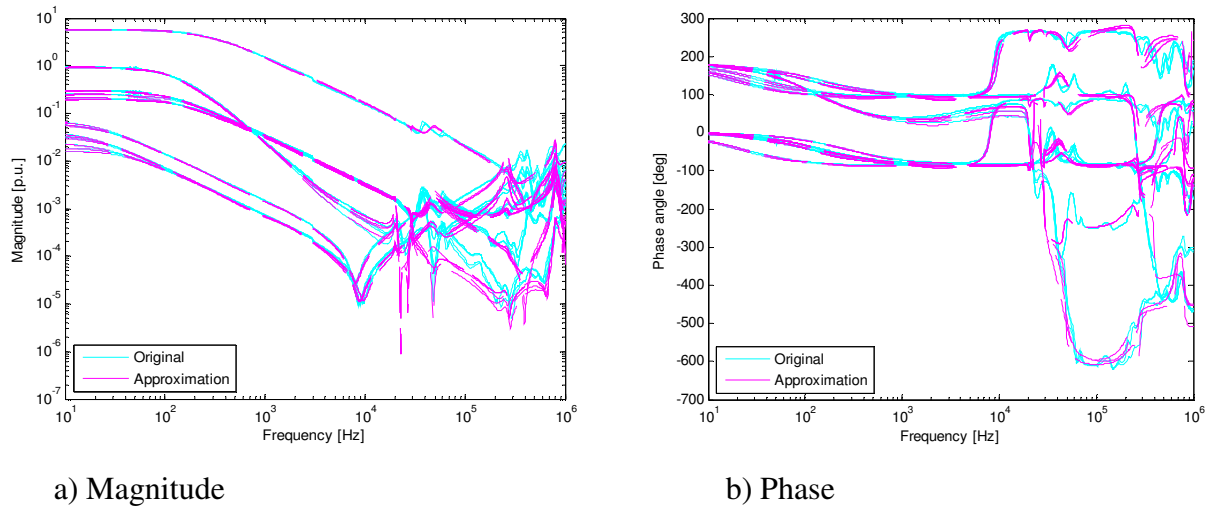


Fig.6.12 Rational approximation of Y for TX2 with $N=20$.

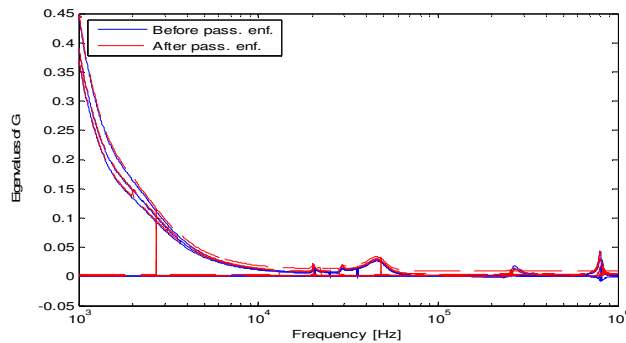


Fig.6.13 Eigenvalues of $\text{Re}\{Y\}$ for TX2 before and after passivity, $N=20$ for 1kHz to 1MHz.

In principle, a perfect fit can be obtained by increasing the order indefinitely high. In practical applications, however, one often wants to find a low order approximation as higher order gives larger element size of the resulting network, higher simulation time and requires very big computational resource. In our case a better fit has been achieved by increasing the order of approximation to $N=100$ with the same passivity enforcement as the previous one. The resulting approximation is shown in Fig.6.14 where it is seen that the approximation has been improved throughout the whole frequency range. The rms-error in this case is 0.0113. The Eigen values of $\text{Re}\{Y\}$ before and after passivity enforcement is given in Fig. 6.15.

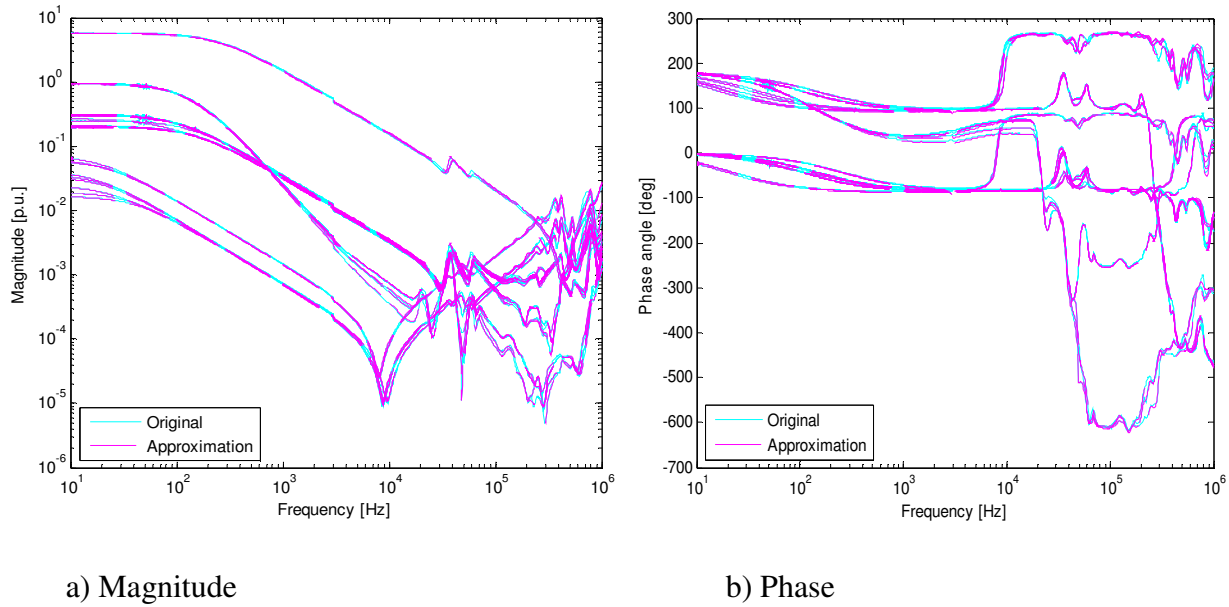


Fig.6.14 Rational approximation of Y for TX2 with $N=100$.

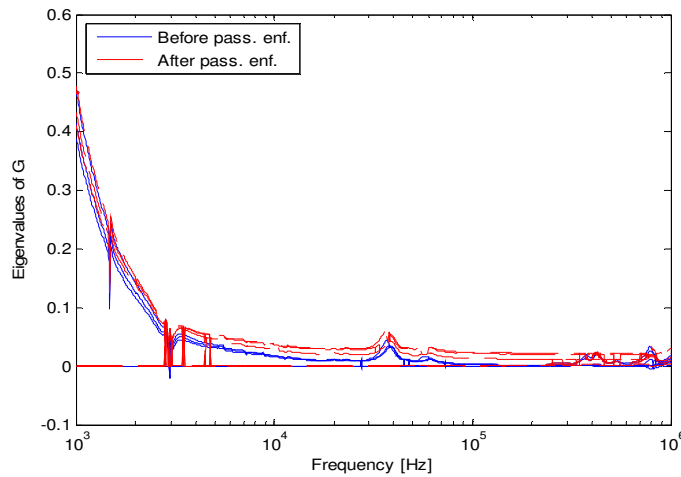


Fig.6.15 Eigenvalues of $\text{Re}\{Y\}$ for TX2 before and after passivity, $N=100$ for 1kHz to 1MHz.

To show the effect of passivity on the fitting error, $Y(s)$ was approximated with order of approximation $N=100$ as in *Fig. 6.14* but with an increased range of frequencies enforced. *Fig. 6.16* gives the Eigen values of $Y(s)$ before and after passivity is enforced over the frequency range 0.1Hz to 10MHz. The error of approximation is increased from 0.0113 to 0.015133. The increase in fitting error is because of perturbation of more frequency points while enforcing passivity in the later case. To decrease the fitting error due to passivity, therefore, very accurate measurements should be made so that there are no passivity violations inside the frequency range of interest or outside. A compromise is therefore made between stability and fitting error.

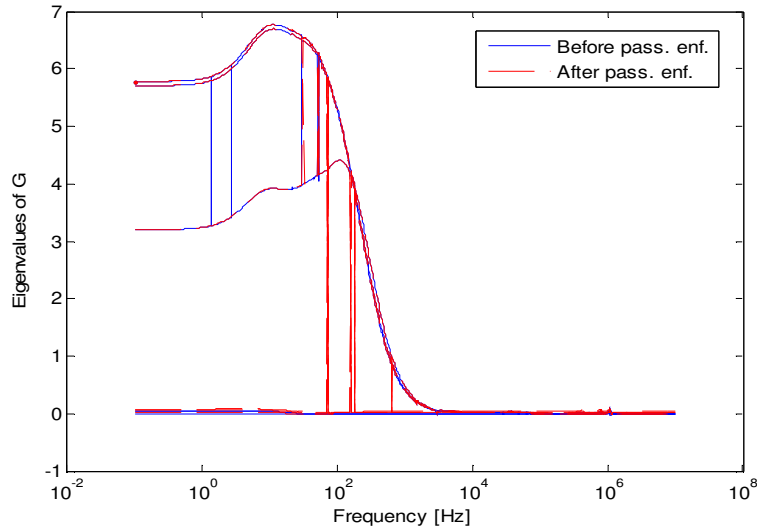
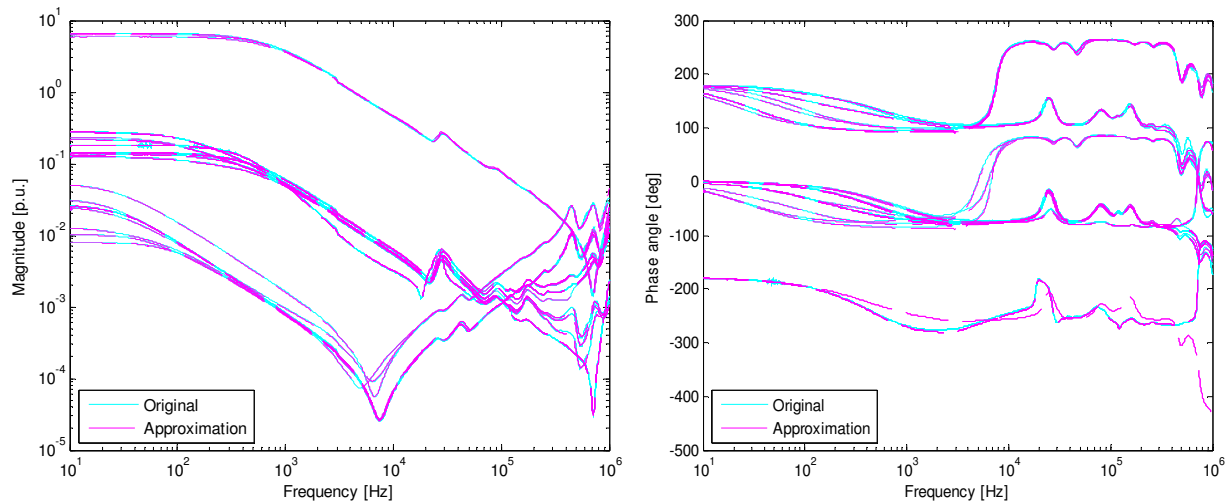


Fig.6.16 Eigenvalues of $Re \{Y\}$ for TX2 before and after passivity, $N=100$ for 0.1Hz to 10MHz.

Fig.6.17 and *Fig.6.18* give the rational approximation and eigenvalues of $Re\{Y(s)\}$ respectively of TX1 for $N=60$ and passivity enforcement over 0.1kHz to 10MHz on 1601 points. The rms-error is 0.023634. A reduced order of approximation was used due to limitation of computational memory since the number of measurement points to be approximated in this case was 1601 which is double that for TX2.



a) Magnitude

b) Phase

Fig.6.17 Rational approximation of Y for TX1 with $N=60$

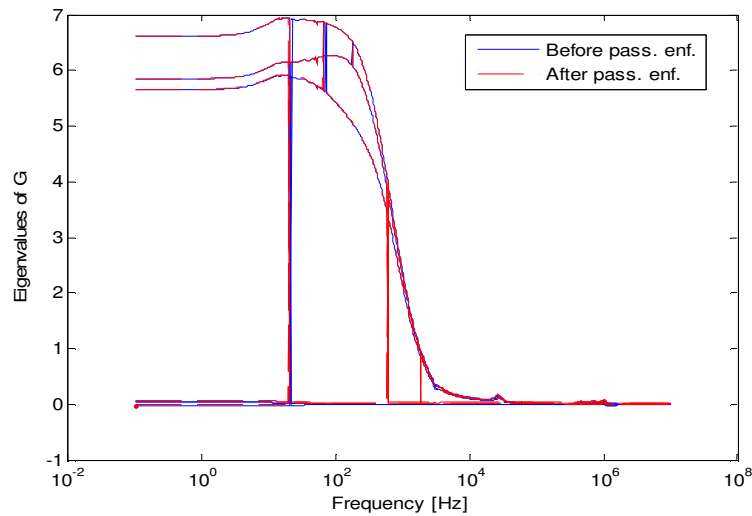


Fig.6.18 Eigenvalues of $Re \{Y\}$ for TX1 before and after passivity, $N=60$ for 0.1Hz to 10MHz.

Finally, approximations and eigenvalues with orders 20 and 100 are plotted for the small transformer at Chalmers as shown in Fig. 6.19, Fig. 6.20, Fig.6.21 and Fig.6.22 respectively. Deviations between original data and approximations are also shown in the same plots. Far better fits are achieved for this transformer since the number of elements to be fitted with a common set of poles in this case is only 4.

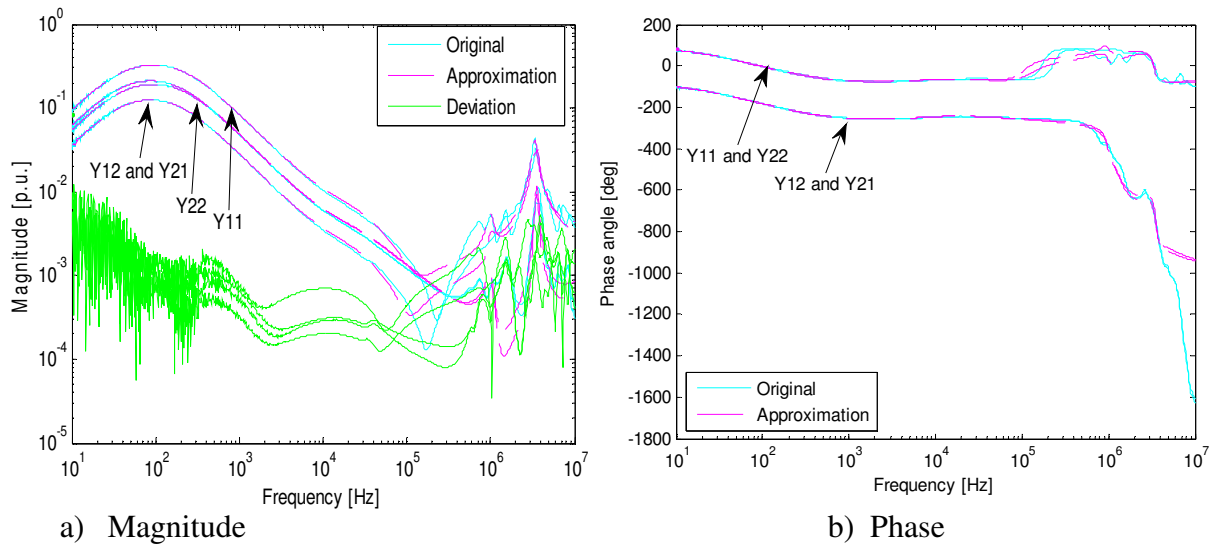


Fig.6.19 Rational approximation of Y for small transformer with $N=20$.

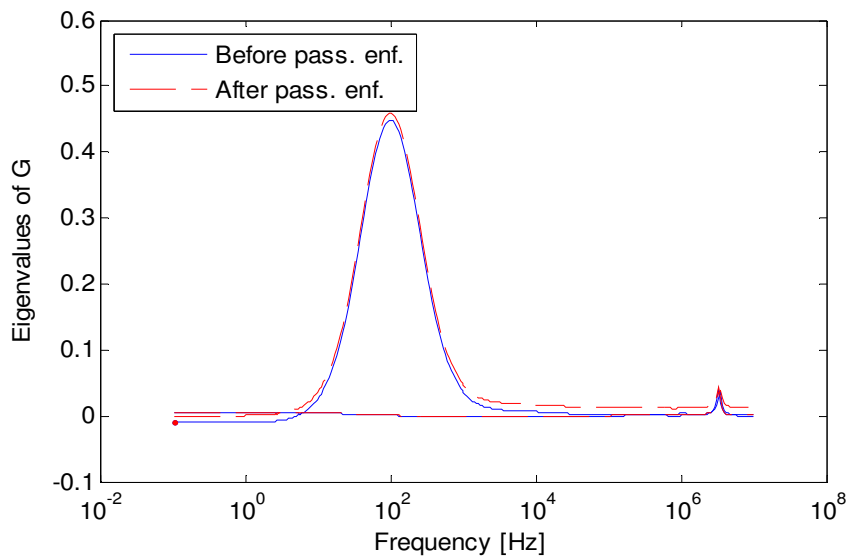
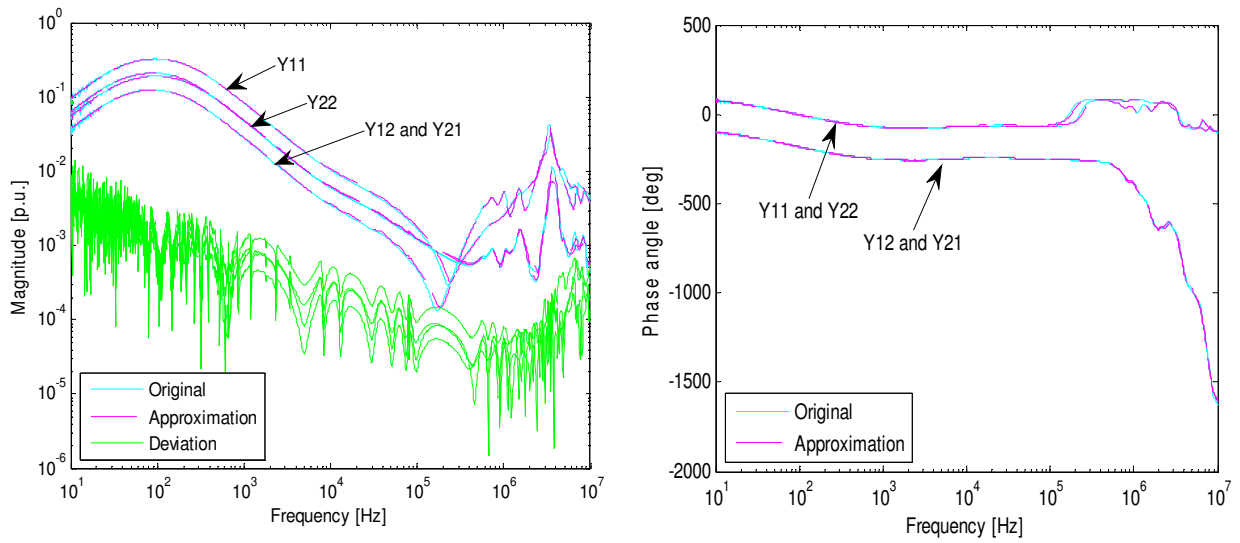


Fig.6.20 Eigenvalues of $\text{Re}\{Y\}$ for small transformer before and after passivity, $N=20$ for 0.1Hz to 10MHz.



a) Magnitude

b) Phase

Fig.6.21 Rational approximation of Y for small transformer with $N=100$.

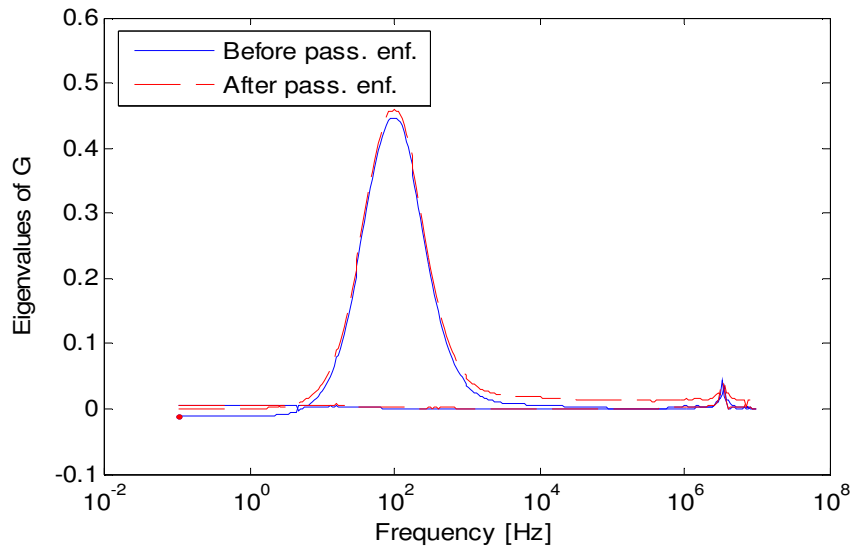


Fig.6.22 Eigenvalues of $Re \{Y\}$ for small transformer before and after passivity, $N=100$ for 0.1Hz to 10MHz.

6.5 Model Validation

In this section the validity of the transformer models has been checked by comparing the voltage ratio measured directly on the transformer terminals with the calculated and simulated by the model in PSCAD/EMTDC. The voltage ratio calculated was obtained from the measured admittance using (5.11) and (5.12). The accuracy of this model greatly depends on the accuracy of the measured admittance and hence it is very important to check if these measurements are accurate enough to give the accuracy requirements to the model to be developed using these measurements. One way to validate the transformer model is therefore to validate the measured admittance matrix without further doing time-domain implementation in PSCAD/EMTDC as this model was formulated in terms of its admittance matrix.

Transformer TX2

The PSCAD/EMTDC simulated result for TX2 was obtained by the model developed for an admittance matrix Y measured with 801 number of frequency samples and fitted with an approximating rational function of order 100. *Fig.6.23* to *Fig.6.26* compares the measured elements of voltage ratio from low to high (V_{LH}) with the corresponding elements calculated and simulated. The calculated ratio is seen to closely match the measured ratio except at lower frequencies. The reason for this will be explained later in section (6.6). Similarly very good agreement has been obtained between the calculated and simulated ratio as it can be seen in the same figures. It is important to note here that as the model developed is not directly from the measured admittance but from rational approximation of the measured admittance, the small deviation between the calculated and simulated are the result of fitting errors otherwise the calculated and simulated curves fall on the same curve provided that we can get an ideal perfect fitting. In practical applications, one often wants to find low order approximation as higher order gives larger element size of the resulting network, higher computer memory and higher simulation time. With the computer we had for example it was impossible to exceed the order from 130 or 80 for number of samples 801 and 1601 respectively.

A similar observation is made for the voltage ratio elements from high to low (V_{HL}) when comparing measured and calculated quantities, see *Fig.6.27* to *Fig.6.29*.

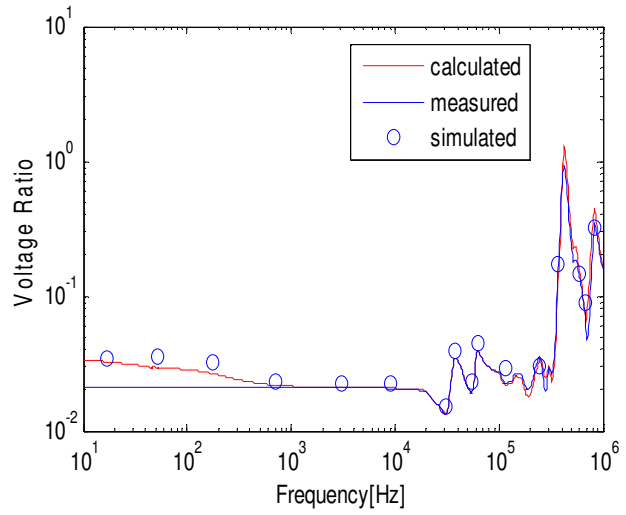
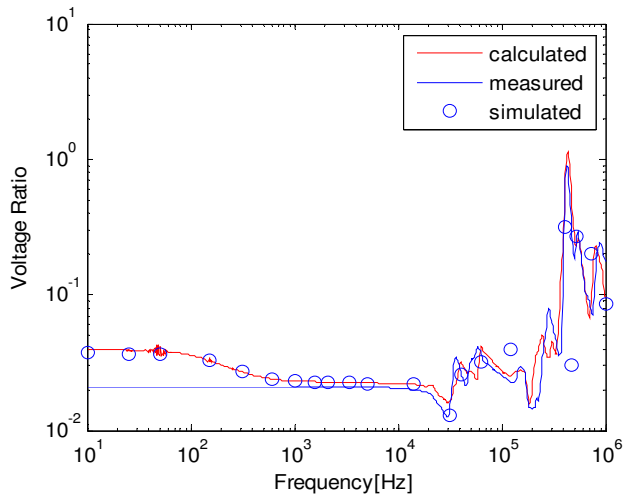


Fig.6.23 Voltage ratio low to high $V_{LH,41} = \frac{V_{L,4}}{V_{H,1}}$. Fig.6.24 Voltage ratio low to high $V_{LH,52} = \frac{V_{L,5}}{V_{H,2}}$.

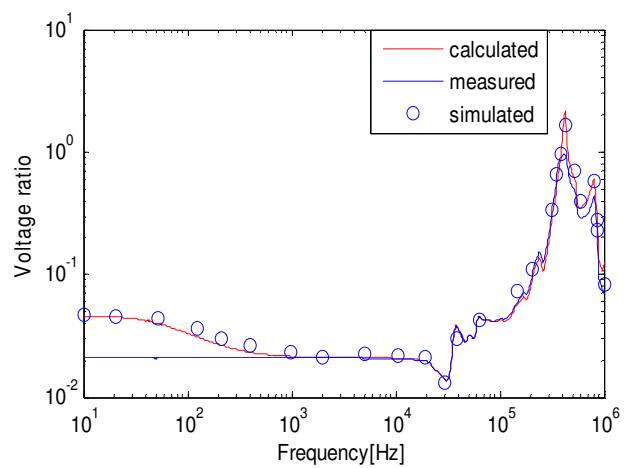
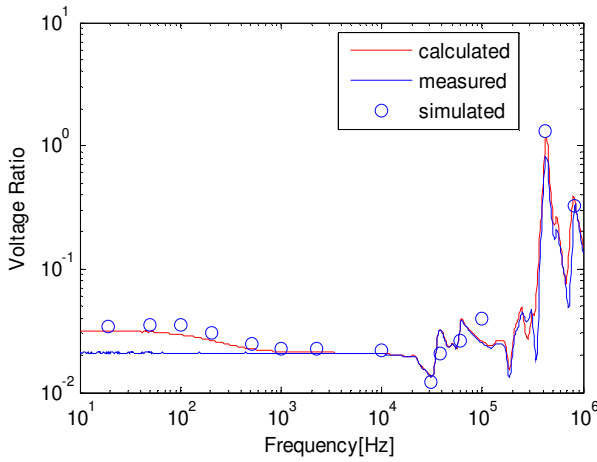


Fig.6.25 Voltage ratio low to high $V_{LH,63} = \frac{V_{L,6}}{V_{H,3}}$. Fig.6.26 Voltage ratio low to high $V_{LH,61} = \frac{V_{L,6}}{V_{H,1}}$.

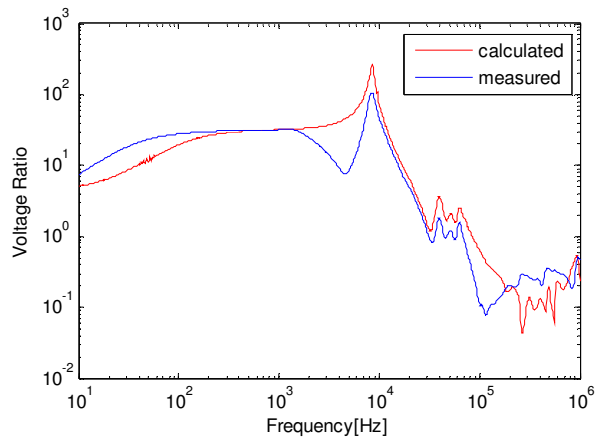
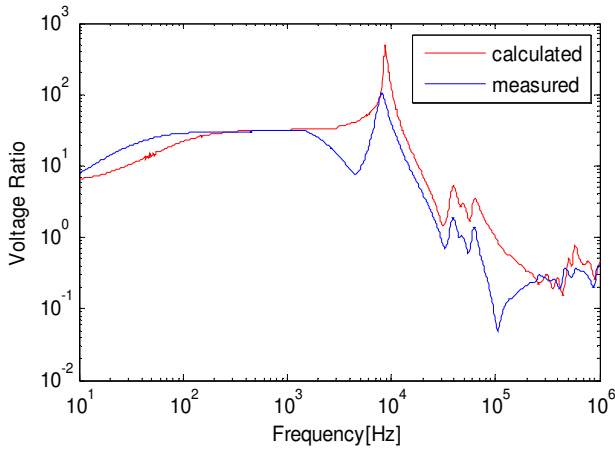


Fig.6.27 Voltage ratio high to low $V_{HL,14} = \frac{V_{H,1}}{V_{L,4}}$. Fig.6.28 Voltage ratio high to low $V_{HL,25} = \frac{V_{H,2}}{V_{L,5}}$.

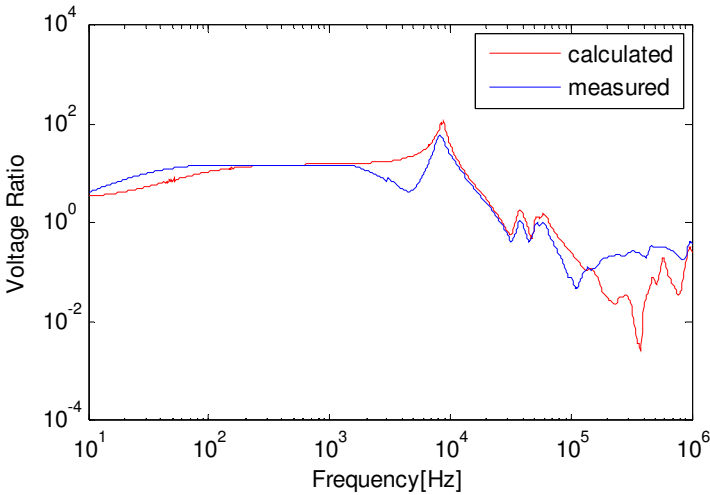


Fig.6.29 Voltage ratio high to low $V_{HL,36} = \frac{V_{H,3}}{V_{L,6}}$.

Transformer TX1

Similar plots have been made for transformer TX1 except the admittance matrix and voltage ratios were measured for 1601 number of samples and the simulated results are for the model obtained with an order of approximation of 60 for the measured admittance. Reasonably good agreement between calculated and simulated results are obtained for the voltage ratios V_{LH} as it is shown in the plots of Fig.6.30 to Fig.6.32. Compared to the results obtained for TX2, it is seen that a relatively large deviation between the measured and calculated (simulated) is observed for TX1. This is due to the higher error on the measured admittance for TX1 than TX2. This was observed during the measurements of the admittance for TX1 where more elements have to be replaced using symmetry of the

matrix. This can also be observed by comparing the admittance matrix plots for TX2 and TX1 shown in Fig.6.8 and Fig.6.9.

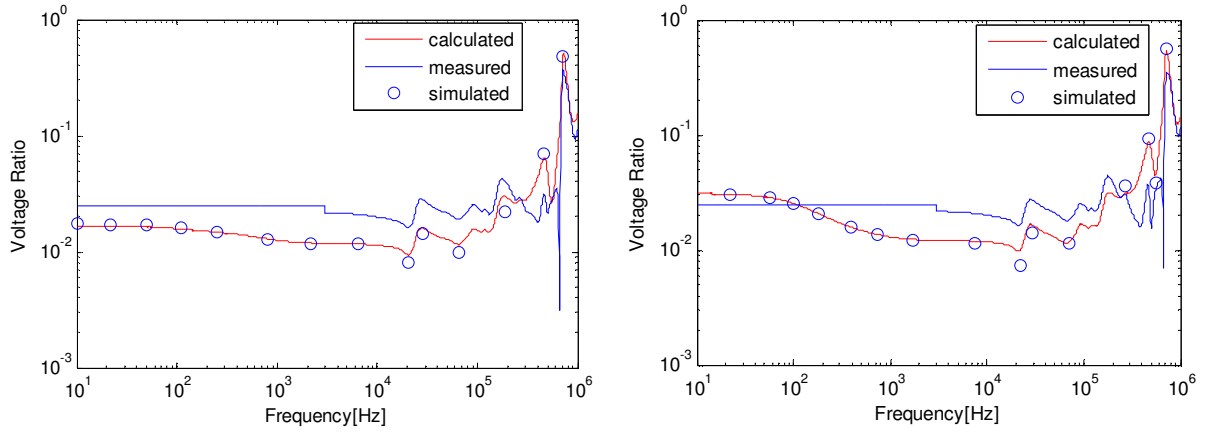


Fig.6.30 Voltage ratio low to high $V_{LH,41} = \frac{V_{L,4}}{V_{H,1}}$. Fig.6.31 Voltage ratio low to high $V_{LH,521} = \frac{V_{L,5}}{V_{H,2}}$.

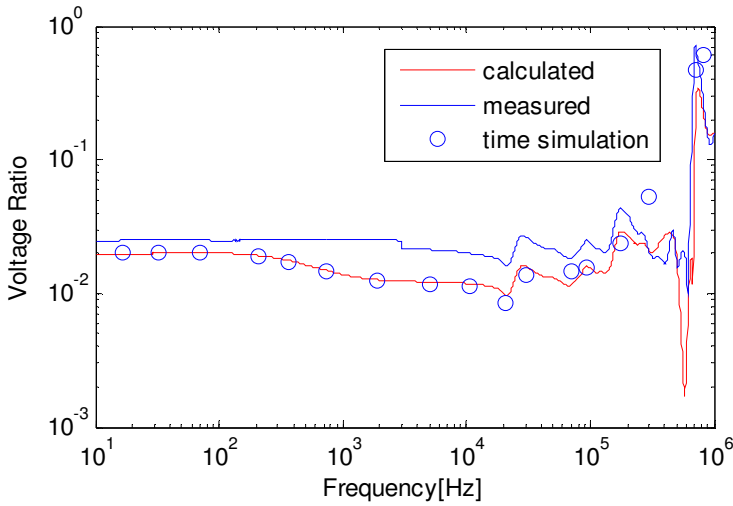


Fig.6.32 Voltage ratio low to high $V_{LH,63} = \frac{V_{L,6}}{V_{H,3}}$.

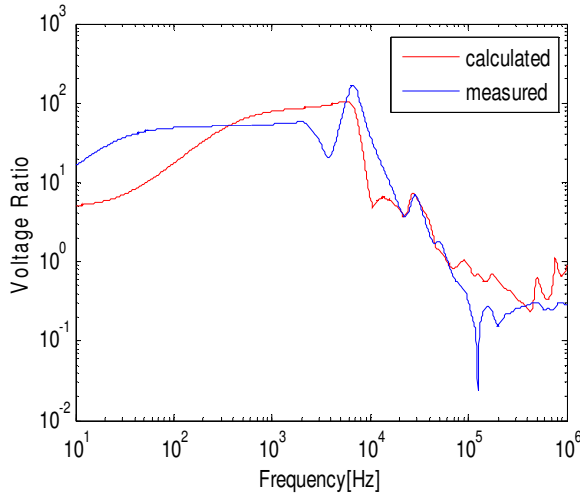


Fig.6.33 Voltage ratio high to low $V_{HL,14} = \frac{V_{H,1}}{V_{L,4}}$.

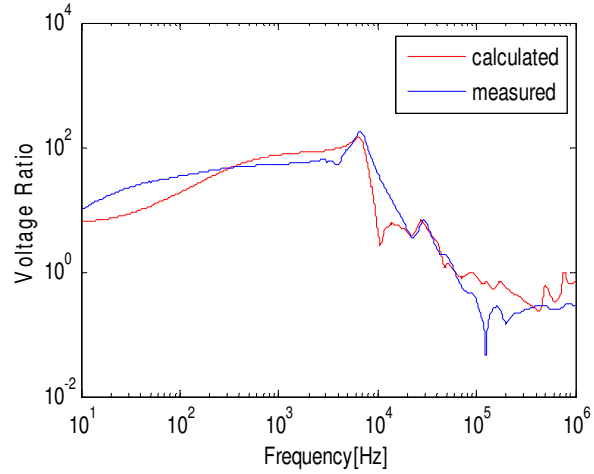


Fig.6.34 Voltage ratio high to low $V_{HL,25} = \frac{V_{H,2}}{V_{L,5}}$.

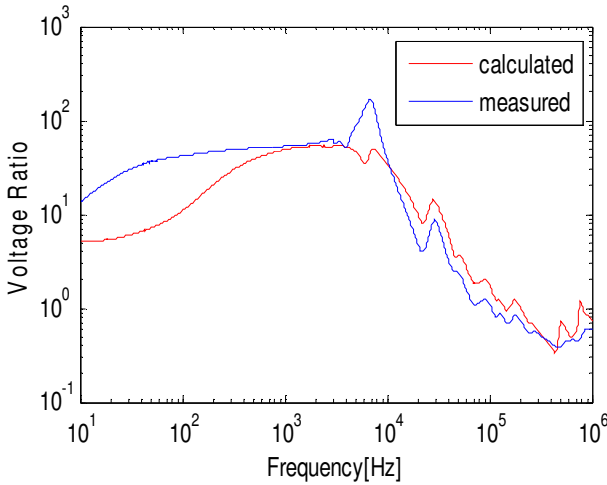


Fig.6.35 Voltage ratio high to low $V_{HL,36} = \frac{V_{H,3}}{V_{L,6}}$.

Single phase Transformer

Fig.6.36 and Fig.6.37 compare the measured and calculated (using (5.11) and (5.12)) values of voltage ratios. The calculated ratios are seen to closely match the measured ratios with some discrepancy. According to [23] the condition with one or more terminals of the transformer open is the worst case scenario because a 1% measurement error in the admittance matrix could cause as high as 100% error in the calculated voltage ratio, hence the errors obtained are reasonable.

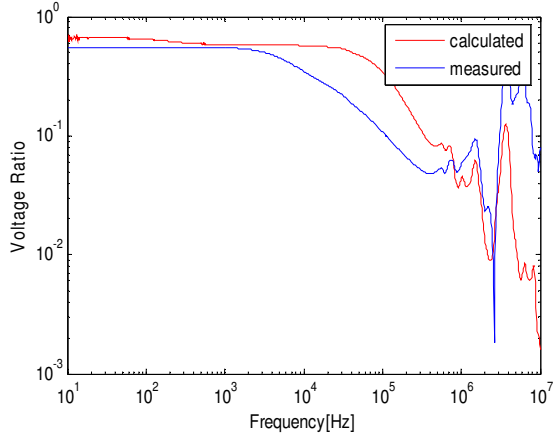
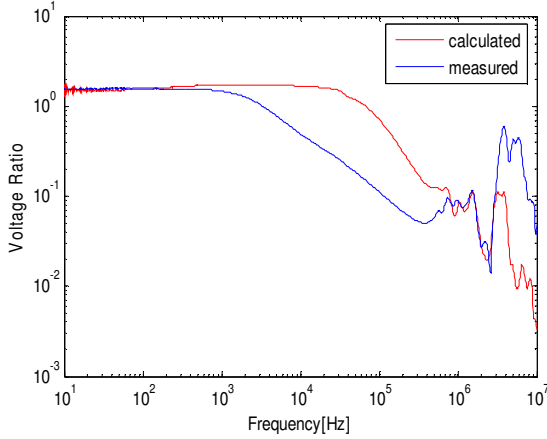


Fig.6.36 Voltage ratio high to low $V_{LH,12} = \frac{V_{L,1}}{V_{H,2}}$. Fig.6.37 Voltage ratio high to low $V_{HL,21} = \frac{V_{H,2}}{V_{L,1}}$.

6.6 Accuracy of the Model

The models developed for TX2 and TX1 are not accurate at lower frequencies. This can be seen from the comparison between measured and calculated results of the preceding sections, see Fig.5.27 to Fig.5.39. This is especially observed for TX2 in plots of Fig.5.27 to Fig.5.33. This error is due to the ungrounded windings of the delta connected high voltage winding for both transformers.

The inaccurate result at low frequencies for transformers with ungrounded windings is due to the inaccuracy in the zero sequence component of the admittance matrix at low frequency corresponding to the ungrounded winding as the capacitive coupling to ground of an ungrounded winding approaches zero with decreasing frequency, thereby causing a near-singular condition for the blocks in the admittance matrix Y associated to ungrounded windings (Y_{HH}, Y_{HL}, Y_{LH}) and hence the zero-sequence component of diagonal and off diagonal blocks associated with ungrounded windings (Y_{HH}, Y_{HL}, Y_{LH}) becomes very small because the current is too small to be accurately determined as the only connection to ground is via capacitors.

The sensitivity of the model to errors in measurements and the rational approximation was also found to be very high when one or more terminals were open-circuited on one or both sides of the transformer. Thus, a transformer model may, in general, produce accurate results in one situation and inaccurate results in a different situation.

6.7 Conclusion

This chapter demonstrated how a linear wide band frequency dependent model of a power transformer has been developed. A dedicated measurement setup to measure the admittance matrix over a wider frequency range has been designed. Vector fitting was adapted to subject the measured admittance matrix to rational function approximation. Network realization of the approximating rational function to its equivalent electrical network generated given in a Matlab generated file was used later to implement the model in a PSCAD script for time domain simulation.

From the admittance matrix measurements taken at two different numbers of samples, the measurement setup was shown to give reproducible results. Comparison of results between measured, calculated and simulated results show good agreement. The model was however found to be sensitive to measurement errors especially for a transformer with ungrounded windings. The errors were magnified at lower frequencies and during open circuit conditions.

Chapter 7

CONCLUSIONS AND FUTURE WORK

7.1 Conclusions

In power systems that comprise an interconnection of cables, VCBs and transformers as in a wind farm, very severe high frequency overvoltages may occur due to the switching action of the VCB. Characterization of these overvoltages and the ultimate protection from them requires accurate modeling of the above components.

The first part of this report dealt with cable modeling and experimental validations. It has been studied that the following conclusions can be drawn:

- With certain adjustments that take into account the semiconducting layers and core and sheath stranding, the Frequency Dependent (Phase) Model provided by PSCAD/EMTDC gives a fairly very good model of a real cable. This model replicates high frequency behaviors like skin effect, reflections, EM propagation.
- The results of the experiment show that good agreements have been achieved between measured and simulated values in the frequency of oscillation and propagation delay. Small disagreements in these parameters are, however, noticed and the authors believe they can be due to unaccounted capacitance of the measuring cables and additional stray capacitances and inductances in the real system. Although it has been found that both simulations and measurements show an increase in damping of the EM transients with increasing frequency of oscillation as it should be, quicker damping is observed in reality than in the simulations.

VCB modeling and characterization of phenomena as current chopping, dielectric with stand and high frequency quenching capability makes the second part of this thesis. The following conclusions are inferred:

- The statistical nature of the arcing time, chopping current, dielectric strength, and quenching capability of a VCB requires that a stochastic model be developed for it.
- Although the VCB has good current interruption characteristics, its ability to interrupt high frequency current zeros causes escalation of steep front

overvoltages on the load side due to reignitions or prestrikes specially when inductive currents are interrupted. This has been demonstrated by using a stochastic VCB model in a generic test circuit.

- The generic test circuit was able to replicate actual VCB characteristics and expected results were obtained by looking into the effects of arcing time, rate of rise of dielectric strength, and high frequency quenching capability.

Finally, a wide band frequency dependent model of a power transformer was developed. This model is suitable for the study of transients induced due to VCB switching or other types which contain a very wide range of frequencies. The following points have been noted:

- Since the model is a linear black box equivalent based on measurements on the terminals as opposed to a detailed model of the internal parts of a transformer, it can only be used in transient studies involving overvoltages at the terminals, surge transfer and how it interacts with other external components during these events.
- The transformer model is a linear passive network equivalent of RLC elements. Therefore, non linearity and core saturation of the transformers have not been accounted for. These characteristics are very pronounced for low frequency overvoltages. However, the model can work well for voltages significantly lower than the transformer rated voltage. In addition at relatively high frequencies where the core excitation flux varies very rapidly, these effects are small and can be neglected. Therefore, for high frequency transients, the model can be a sufficient representation.
- It has been tried to validate the model developed by studying voltage transfer from the delta side to the wye side and vice versa. Although good agreements were obtained between voltage ratios calculated from the measured admittance matrix, simulated voltage ratios and those directly measured as function of frequency, there are discrepancies at lower frequencies. These errors are due to the ungrounded windings of the delta side which produces very small zero sequence components of elements associated with this winding at low frequencies.

7.2 Future Work

A lot could be done to get an improved and more accurate model of the components especially the transformer.

Cable Model

The cable model simulates most of the characteristics of a real cable and this was verified to measurements on real cable. However the damping of the real cable was found to be higher than the PSCAD/EMTDC model besides the model doesn't take in to account the presence of the armour. Hence more work could be done to get much more accurate model in this regard.

VCB Model

The VCB model in this project simulates most of the phenomena of a real breaker very accurately and hence the authors feel it is good enough for its purpose. However a more accurate model can still be obtained by considering more aspects that were not dealt in this work.

Transformer Model

It was seen that the transformer model developed in this work is not accurate at lower frequencies; hence more work should be done to get a refined and robust model by taking in to account a lot of aspects that were not taken in to consideration on this work. The following is suggested:

Improving the measurement set up

The accuracy of this model depends on the accuracy of the measured admittance matrix and hence accurate measurement is required as the model is very sensitive to error in measurement.

One way to improve the accuracy of the measured data is by designing Special measurement setup dedicated to measure the admittance matrix and voltage ratio which allow easily reconnection and accurate measurement. One problem faced in this work was the measurement set up was so simple that it doesn't allow easily reconnection. Reconnection has to be made every time a single element of the admittance matrix or voltage ratio was measured. For the three phase transformer with 36 admittance matrix and 9 voltage ratio elements for example 45 different connections was made. This was time consuming not mentioning its effect on the accuracy of the data set due to bad connection and inconsistency in the length of the connection cable used. This was reflected on the measurements obtained on the admittance and voltage ratio. Besides the simple connection cables used has greatly contributed to the measurement error. This was also seen during measurements where some elements of the admittance matrix and especially voltage ratio were very noisy. To deal with this problem the cables to be used in future work should be shielded.

Measuring the Zero sequence Admittance

In accuracy of the model at lower frequencies for a transformer with ungrounded windings like the transformers we dealt with can be overcome by explicit measurement and modelling of the zero sequence system. Blocks of Y , which correspond to ungrounded windings (Y_{HH}, Y_{HL}, Y_{LH}), are modified by removal of their zero sequence components as the zero sequence component of the admittance matrix is inaccurate due to small zero sequence current. A new zero sequence system has to be obtained by dedicated measurements and the two functions can then be approximated with rational functions which can be combined to produce the final model. In this work we have tried to measure the zero sequence admittance though we didn't succeed to get accurate measurement.

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APPENDICES

Appendix A. Implementation of 3-phase Transformer model in PSCAD/EMTDC

In this appendix the procedure for implementing the transformer model developed in this thesis in transient time simulation software PSCAD/EMTDC is demonstrated.

The out put of the main Matlab source code is either a state space equivalent or a file of branch cards of an equivalent RLC network of the transformer. The later can be used directly in PSCAD/EMTDC or other time simulation packages to build the transformer component. A branch based interface was used to define the branches of the equivalent network. Branch design is accomplished by specifying the type and size of passive elements (i.e. lumped R, L and/or C), and to which electrical connections they fall between. The component definition is written as a script in the format

$$\text{\$<TO> \$<FROM> \quad [<R>] \quad [<L>] \quad [<C>]}$$

where $\text{\$<TO>}$ and $\text{\$<FROM>}$ refer to the branch end nodes and $[<R>]$, $[<L>]$, $[<C>]$ to the passive element values in Ohm, Henry and micro Farad respectively.

Nested page modules are used to build the model as the number of branches is too big to implement as a single component. Therefore each one of the big branches between two nodes or between a node and ground is modeled as sub modules which are then connected to form the whole network.

The steps are summarized as follows:

1. Create a new component page module in the circuit page with 3 connections on the left, 3 on the right and one at the bottom, ground to model the whole equivalent network as in *Fig. A.1*.
2. Double click on the newly created page module and create components corresponding to each one of the big branches. Connect these blocks between corresponding nodes (connections) referred in 1 as shown in *Fig. A.2*.

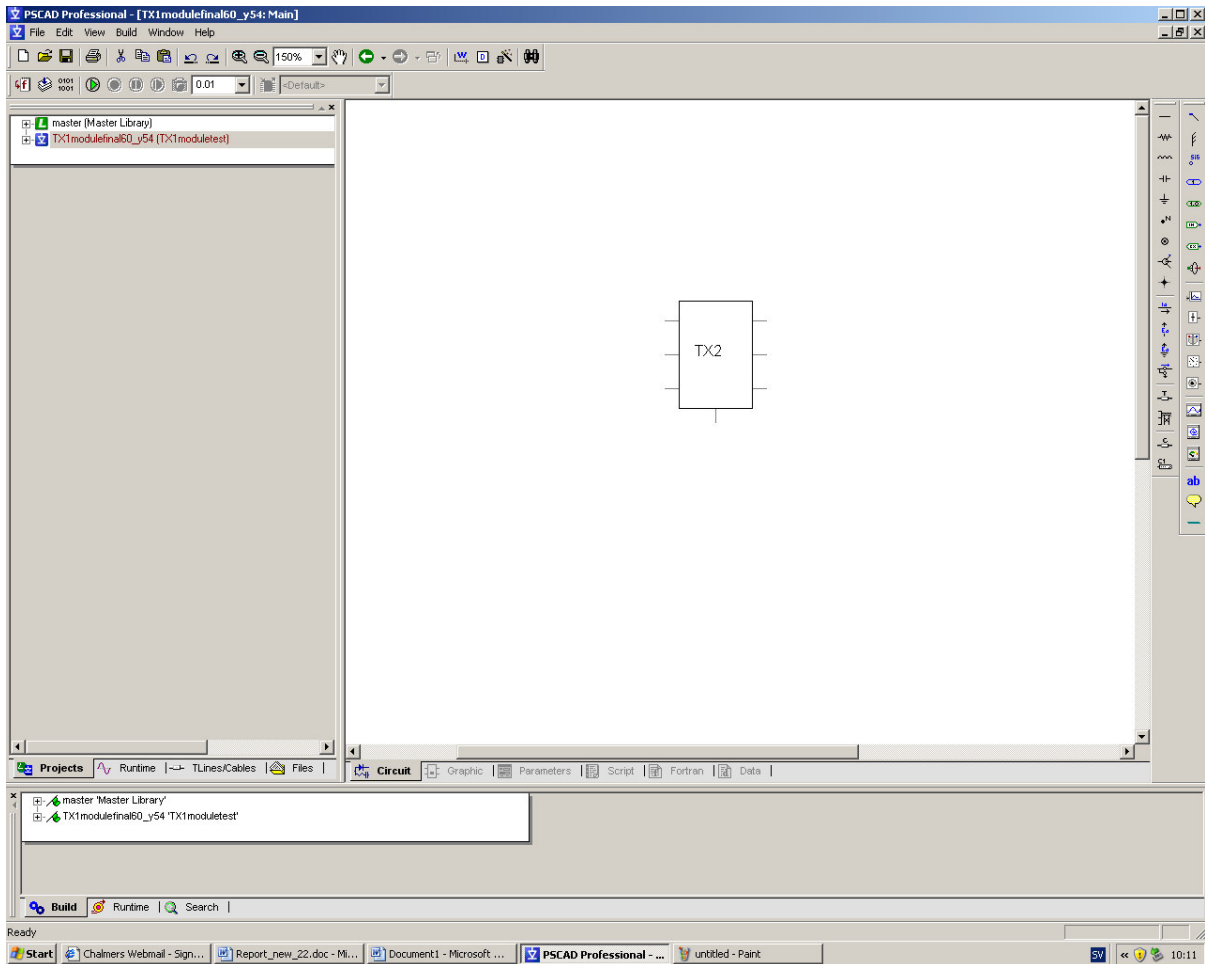


Fig. A.1 Transformer component page module.

3. Enter component definitions for each one of the components in 2 as script. A typical script page would look like as in *Fig. A.3*.

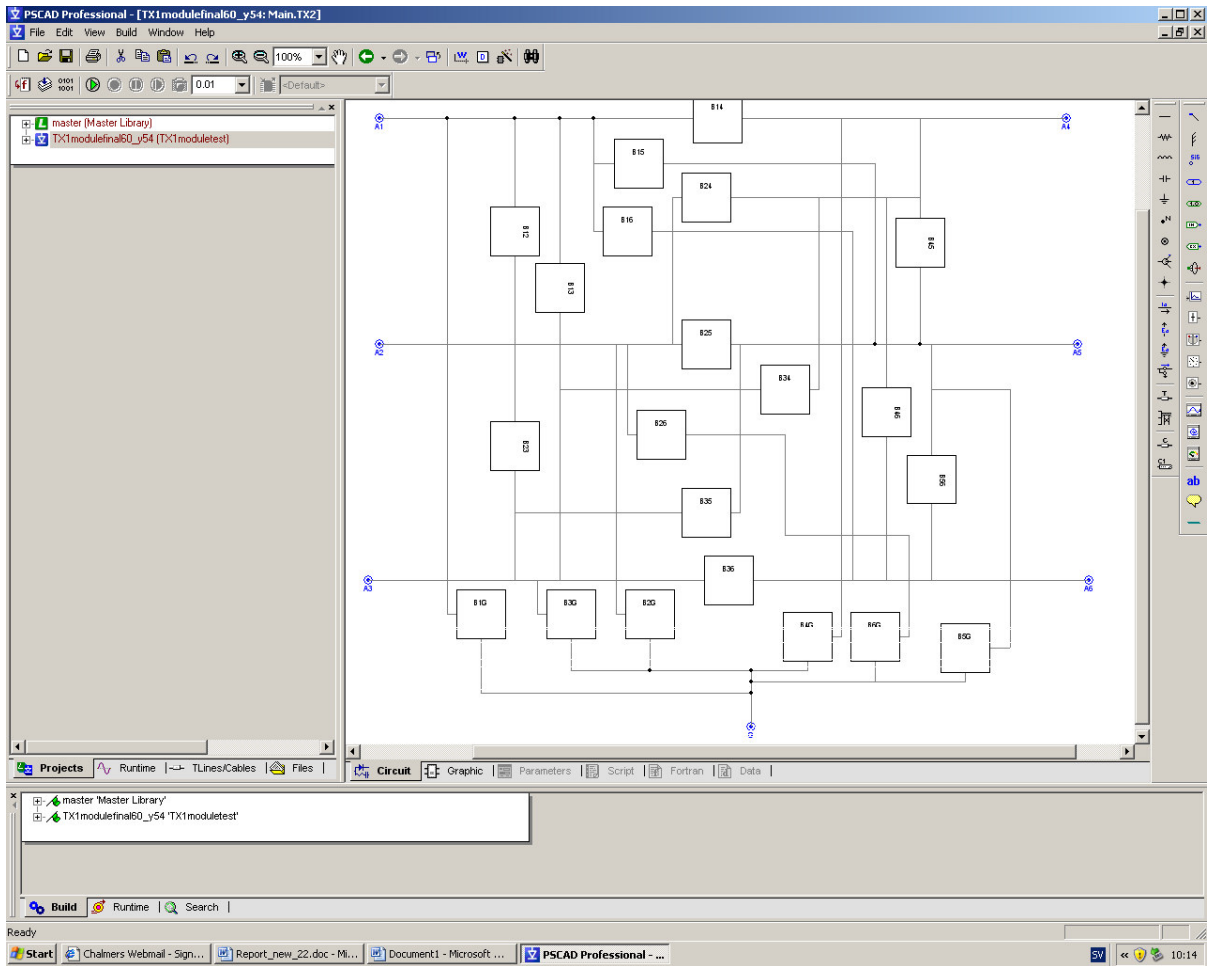


Fig. A.2 Components corresponding to internode branches.

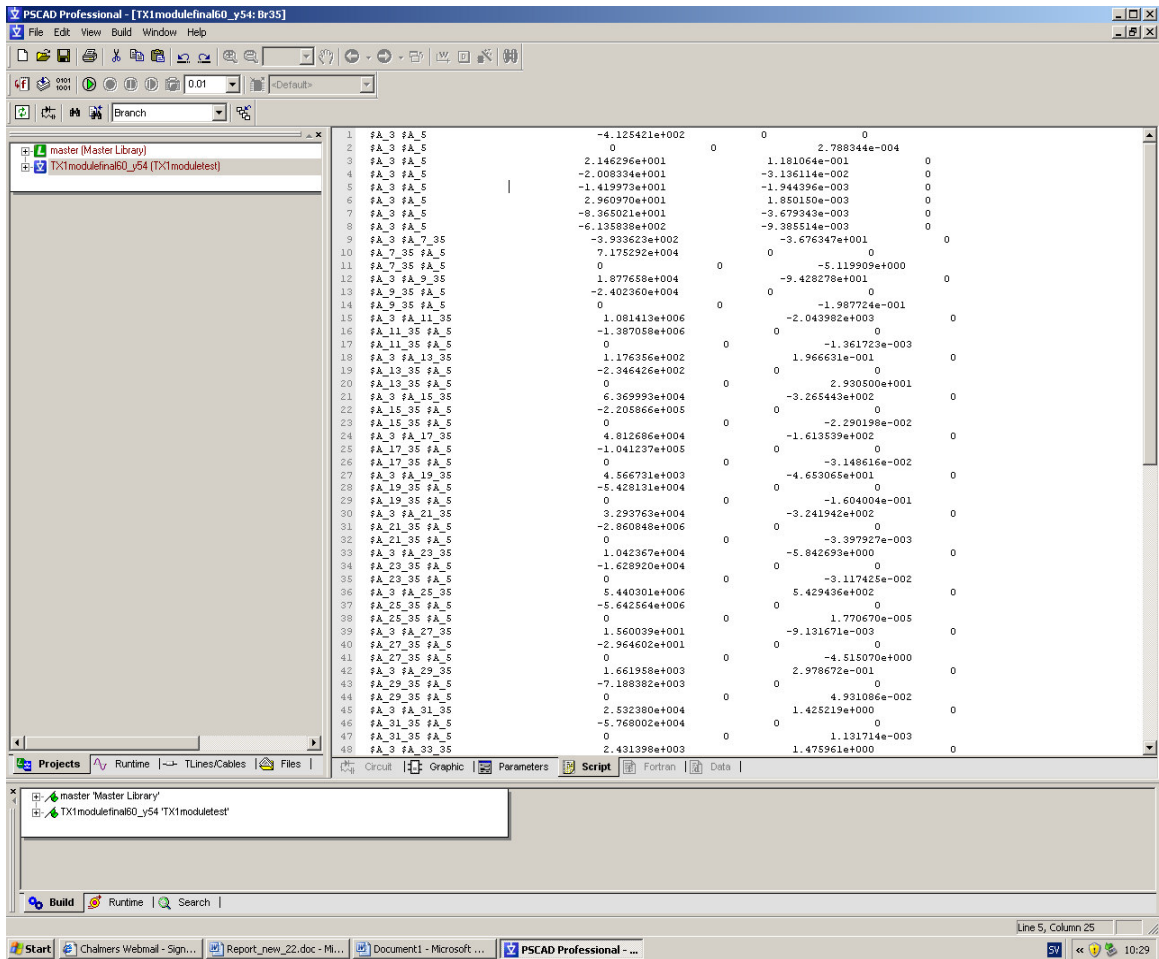


Fig. A.3 Component definition as script page.

Appendix B. Network Realization

Consider the multi-terminal network shown in *Fig.B.1* the admittance matrix for this network can be computed as

A diagonal element Y_{ii} of the admittance matrix is obtained as the sum of admittances for all branches connected to terminal i , including branches to ground, i.e.,

$$Y_{ii} = y_i + \sum_{j=1, j \neq i}^n y_{ij} \quad (1)$$

The off-diagonal elements are the negative of the admittances connecting buses i and j i.e.,

$$Y_{ij} = -y_{ij} \quad (2)$$

Where y_i denotes the admittance of a branch connected between terminal i to ground and y_{ij} admittance connected between terminal i and j .

Given the admittance matrix we can also compute the admittance of the branches connected between terminals and a terminal to ground.

From (2) the admittance of the branch connected between terminal i and j may be written as

$$y_{ij} = -Y_{ij} \quad (3)$$

Similarly the branch between terminal i to ground can be computed from (1)

$$y_i = Y_{ii} - \sum_{j=1, j \neq i}^n y_{ij} \quad (4)$$

If the value of y_{ij} from (2) is replaced in to (4) then

$$y_i = Y_{ii} + \sum_{j=1, j \neq i}^n Y_{ij} \quad (5)$$

We may write (5) in compact form according to:

$$y_i = \sum_{j=1}^n Y_{ij} \quad (6)$$

Given the admittance matrix of a device in frequency domain the corresponding network can easily be obtained connecting branches between terminals and terminal to ground by realizing the admittances obtained from (3) and (6). This gives a network of the form shown in *Fig.B.1*.

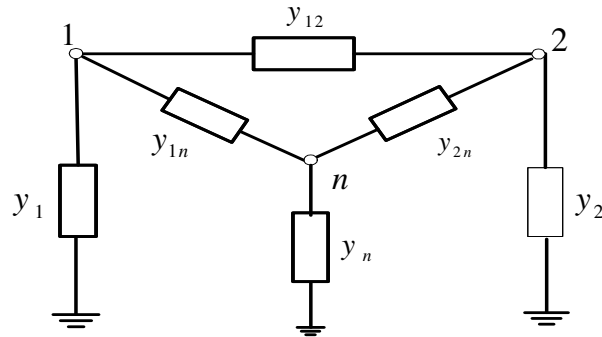


Fig.B.1 Multi- terminal network equivalent of a device.

Fundamentals of Network Synthesis

A network is represented by a rational function in s-domain. This rational function is called network function. Network functions are expressed in terms of the complex frequency variable s , resulting from the application of Laplace transformation to time domain network equations. This network functions are either impedance or admittance. Given the impedance or admittance function then it possible to find the network representation.

As a passive net work is an inter connection of the basic passive elements; resistor, capacitor, and inductor; let's start by driving the network function of this elements which is the basic for synthesis of a complex network including the network we are trying to find for the transformer model.

The voltage and current at the terminals of these elements in time domain t and frequency domain s is given in Table B.1 is given by

Table B.1 Voltage and current relation ship of passive elements

	RESISTOR	CAPACITOR	INDUCTOR
Relation ship between voltage and current in time domain	$v(t) = Ri(t)$ $i(t) = Gv(t)$	$v(t) = \frac{1}{C} \int_0^t i(x) dx + v(0^-)$ $i(t) = C \frac{dv(t)}{dt}$	$v(t) = L \frac{di(t)}{dt}$ $i(t) = \frac{1}{L} \int_0^t v(t) dt + i(0^-)$
Relation ship between voltage and current in frequency domain	$V(S) = RI(S)$ $I(S) = GV(S)$	$V(s) = \frac{1}{SC} I(S) + \frac{v(0^-)}{S}$ $I(S) = C[SV(S) - v(0^-)]$	$V(S) = L[SI(S) - i(0^-)]$ $I(s) = \frac{1}{SL} V(S) + \frac{i(0^-)}{S}$

The impedance and admittance functions are defined as the ratio of voltage to current transform and current to voltage transformer.

$$Z(S) = \frac{V(S)}{I(S)} \quad (7)$$

$$Y(S) = \frac{I(S)}{V(S)} \quad (8)$$

If the initial conditions in Table.B.1 are zero then the impedance and admittance functions of the elements can easily be computed (7) and (8).

Table B.2 Network function of the basic elements

	RESISTOR	CAPACITOR	INDUCTOR
Impedance Z(S)	$Z(S) = \frac{V(S)}{I(S)} = R$	$Z(S) = \frac{V(S)}{I(S)} = \frac{1}{CS}$	$Z(S) = \frac{V(S)}{I(S)} = LS$
Admittance Y(S)	$Y(S) = \frac{I(S)}{V(S)} = G$	$Y(S) = \frac{I(S)}{V(S)} = CS$	$Y(S) = \frac{I(S)}{V(S)} = \frac{1}{LS}$

Suppose Y(s) represent the admittance function of one of the branches of n-terminal network representation of the Fig.B.1 and assume that it can be written in partial fraction expansion of the form

$$Y(S) = \sum_1^N \frac{r}{S-a} + d + S.e \quad (9)$$

$$Y(s) = \frac{r}{s-a} + \frac{r_1' - jr_1''}{s - (a_1' - ja_1'')} + \frac{r_1' + jr_1''}{s - (a_1' + ja_1'')} + \frac{r_2' - jr_2''}{s - (a_2' - ja_2'')} + \frac{r_2' + jr_2''}{s - (a_2' + ja_2'')} + \dots + d + s.e \quad (10)$$

$$Y(s) = \frac{r}{s-a} + \frac{2r_1'S - 2r_1'a_1' - 2r_1''a_1''}{s^2 - 2a_1'S + a_1'^2 + a_1''^2} + \frac{2r_2'S - 2r_2'a_2' - 2r_2''a_2''}{s^2 - 2a_2'S + a_2'^2 + a_2''^2} + \dots + d + s.e \quad (11)$$

The network function in (11) can be realized in to its corresponding network. Each part represent admittance of an element or combination of elements and the final network can be obtained by connecting these branches in parallel as admittance in parallel sum up.

We can further simplify (12) by

$$Y(S) = Y_1(S) + Y_2(S) + Y_3(S) + Y_4(S) + Y_5(S) + \dots \quad (12)$$

where

$$Y_1(s) = d$$

$$Y_2(S) = S.e$$

$$Y_3(S) = \frac{r}{S-a}$$

Now let's realize each section starting from the simplest $Y_1(s)$

From Table.B.1

$Y_1(s) = d$, represents admittance of a resistor with a resistance value of $R = \frac{1}{d}$

$Y_2(S) = e.S$, represents admittance of a capacitor with a capacitance value of $C = e$

One can write $Y_3(S)$ as

$Y_3(S) = \frac{1}{\frac{1}{r}S - \frac{a}{r}} = \frac{1}{Z_3(S)}$, where $Z_3(S) = \frac{1}{r}S - \frac{a}{r}$ is an impedance function representing

a series combination of an inductor with an inductance value of $L = \frac{1}{r}$ and a resistor with

a resistance value of $R = \frac{-a}{r}$ as impedances in series sum up.

$$Y_4(S) = \frac{2r_1'S - 2r_1'a_1' - 2r_1''a_1''}{s^2 - 2a_1'S + a_1'^2 + a_1''^2} = \frac{1}{\frac{1}{2r_1}S + \frac{a_1'r''}{2r_1'^2} - \frac{a_1'}{2r_1'} + \frac{1}{\frac{2r_1'}{a_1'^2(1 + \frac{r_1''^2}{r_1'^2})S - \frac{2r_1'a_1' - 2r_1''a_1''}{a_1'^2(1 + \frac{r_1''^2}{r_1'^2})}}} \quad (13)$$

The above equation can be written as

$$Y_4(S) = \frac{1}{Z_4(S) + Z_5(S)}$$

$Z_4(S)$ and $Z_5(S)$ are in series and each can be realized as follows

$Z_4(S)$ is a series combination of an inductor with a resistor whose values can be computed as follows

$$Z_4(S) = \frac{1}{2r_1} \cdot S + \frac{a''r''}{2r_1'^2} - \frac{a_1'}{2r_1'} \quad (14)$$

(14) can be written as:

$$Z_4(S) = LS + R \quad (15)$$

Equating (14) and (15) gives the values of L and R as

$$L = \frac{1}{2r_1}, R = \frac{a''r''}{2r_1'^2} - \frac{a_1'}{2r_1'}$$

$$Z_5(S) = \frac{1}{\frac{2r_1'}{a''^2 \left(1 + \frac{r_1''^2}{r_1'^2}\right)} S - \frac{2r_1'a' - 2r_1''a_1''}{a''^2 \left(1 + \frac{r_1''^2}{r_1'^2}\right)}} \quad (16)$$

Similarly if (16) is rearranged as

$$Z_5(S) = \frac{1}{CS + G} \quad (17)$$

Then $Z_5(S)$ can be realized as a parallel combination of a capacitor and a resistor whose values can be computed by equating (16) and (17).

$$C = \frac{2r_1'}{a''^2 \left(1 + \frac{r_1''^2}{r_1'^2}\right)}, G = -\frac{2r_1'a' - 2r_1''a_1''}{a''^2 \left(1 + \frac{r_1''^2}{r_1'^2}\right)}$$

The final network will then look like:

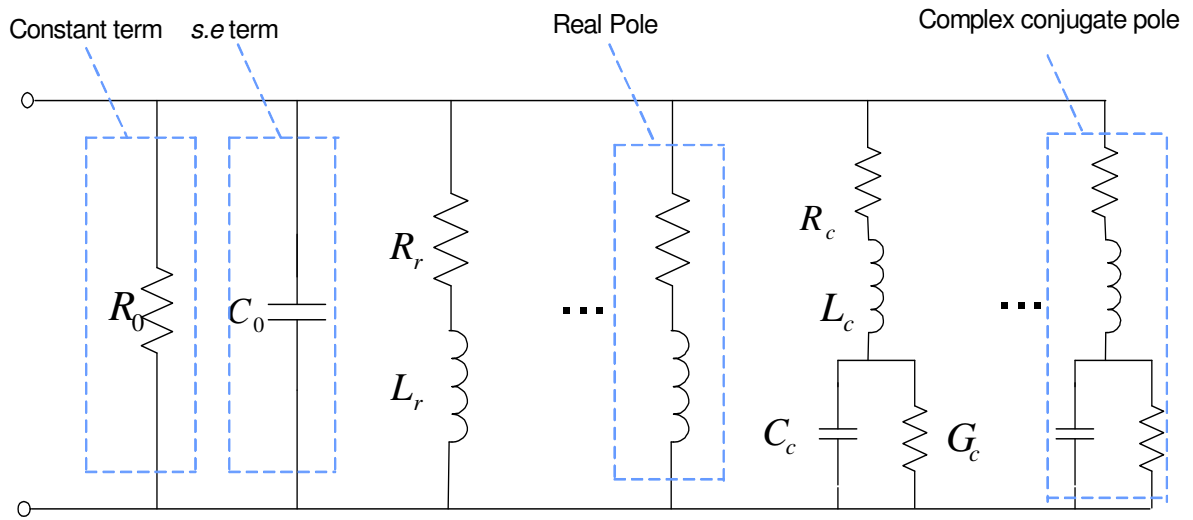


Fig.B.2 Network realization of $Y(s)$.