

1)1-i, 2-h, 3-f, 4-c, 5-a

2a) Sorted elements =

[0 0 0 0 0 0 0 0 0 0 32 38 39 39 41
45 45 47 48 49 50 52 55 58 59 65 75 99] → Median = 41

2b)

$$\log_2(x) = \log_e(x) / \log_e(2)$$

$$Y = e^{\log_2(x)} = e^{\log_e(x) / \log_e(2)} = x^{1/\log_e(2)} \approx x^{1.44}$$

$$x^{1.44} < x \text{ for } x \in (0,1) \rightarrow \text{image will be darker}$$

2c) $H(u,v) = 2 + 2j \cdot \sin(u - v)$

2d) For Sobel filter: gradient magnitude= 2.8 \approx 3 , gradient orientation = 135°

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%-----
hSobel = fspecial('sobel')           % horizontal Sobel filter
vSobel = hSobel'                     % vertical Sobel filter
gradientY = imfilter(I,vSobel);
gradientX = imfilter(I,hSobel);
gradientMagnitude = sqrt(gradientY.^2 + gradientX.^2);
gradientDirection = atan2(gradientY, gradientX);
answer = [ gradientMagnitude(3,3) gradientDirection(3,3)*180/pi]
```

3a) GLCM size: 2 x 2

3b) GLCM

	0	1
0	P(0,0)	P(0,1)
1	P(1,0)=P(0,1)	P(1,1)

The only possibility that entropy=0 is when P(0,0)=1 xor P(1,1)=1.

GLCM solution #1:	GLCM solution #2:																		
<table><tr><td></td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr></table>		0	1	0	1	0	1	0	0	<table><tr><td></td><td>0</td><td>1</td></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td></tr></table>		0	1	0	0	0	1	0	1
	0	1																	
0	1	0																	
1	0	0																	
	0	1																	
0	0	0																	
1	0	1																	
Image: all pixels = 0	Image: all pixels = 1																		

3c)

GLCM

	3	4
3	0	10
4	10	0

GLCM normalized

	3	4
3	0	1/2
4	1/2	0

$$\text{Contrast} = (-1)^2 \cdot \frac{1}{2} + (1)^2 \cdot \frac{1}{2} = 1$$

3d) *Unsupervised* classification: do not use/require training data.

Supervised classification: use information from training data.

4a) When rotating an object by some degrees, the radius (distance to the origo) is preserved: $r^2 = x^2 + y^2 = (x')^2 + (y')^2 = (r')^2$. Here, x', y' are coordinates of the rotated object $\rightarrow \sum_{x,y} (x^2 + y^2) f(x, y) = \sum_{x,y} r^2 f(x, y) = \sum_{x',y'} (r')^2 f(x', y')$

4b) $M = \text{NCOLS} = \text{number of layers}$

$n = \text{NROWS} = \text{number of nodes in a layer}$

Ratio between number of paths to evaluate in DP and Exhaustive computation:

$R = n^M / (n^2(M - 1) + n) \rightarrow \text{DP ca } R \text{ times faster.}$

4c) *sensitivity* = probability of classifying object's pixels as object

specificity = probability of classifying background's pixels as background

4d) The mean shift filtering is a part of the mean shift segmentation algorithm.

4e) The constant λ controls the smoothness of the resulting velocity field. A large lambda corresponds to small changes in the velocity field for the neighboring pixels.

4f) A live-wire is a piecewise-boundary detection technique, and less automatic than snake. A snake requires an initialization only, the live-wire requires the user intervention for every piece of the boundary.

4g) 1p.

5a) See the textbook, Hough transform for circular objects.

5b) A vote matrix with only one vote for every angle/parameter value.

6a) The optimal threshold corresponds to the intersection of the histograms/pdfs:

$$\begin{cases} y = -x + 120 \\ y = -\frac{3}{2}x - 150 \end{cases} \Rightarrow \mathbf{x = T_{opt} = 108} \text{ (optimal threshold value) } y_{opt} = 12$$

$A1 = \text{Area Triangle \#1} = 60 \cdot 60$, $A2 = \text{Area Triangle \#2} = 0.5 \cdot 50 \cdot 30$,

$E = \text{Area of Error triangles} = 10 \cdot 12$

Error rate = $E / (A1 + A2) = (10 \cdot 12 / (60 \cdot 60 + 0.5 \cdot 50 \cdot 30)) = \mathbf{0.0276}$ (2.76%)

6b) Cumulative costs:

	1	2	3
1	20	20	19
2	12	11	14
3	6	12	14
4	6	10	15
5	4	8	15
6	4	10	18

Three minimal paths (with cost =14):

4-10-14; path = (1,5) \rightarrow (2,4) \rightarrow (3,3)

6-12-14: path = (1,4) \rightarrow (2,3) \rightarrow (3,2)

6-11-14: path = (1,3) \rightarrow (2,2) \rightarrow (3,2)