

Solution

the histogram (hit/hough/accumulation) matrix is constructed:

	-3	-2	-1	0	1	2	3
0							
$\pi/4$							
$\pi/2$							
$3\pi/4$							

For each point on a strong edge we find the lines that it may belong to:

For the point $P1(2,2)$ and q :

$$0: \quad r = 2 * \cos(0) + 2 * \sin(0) = 2$$

\Rightarrow line $[2,0]$

$$\pi/4: \quad r = 2 * \cos(\pi/4) + 2 * \sin(\pi/4) = 2.8284 \sim 3$$

\Rightarrow line $[3,\pi/4]$

$$\pi/2: \quad r = 2 * \cos(\pi/2) + 2 * \sin(\pi/2) = 2$$

\Rightarrow line $[2,\pi/2]$

$$3\pi/4: \quad r = 2 * \cos(3\pi/4) + 2 * \sin(3\pi/4) = 0$$

\Rightarrow line $[0,3\pi/4]$

So the histogram matrix is updated as follows:

	-3	-2	-1	0	1	2	3
0						/	
$\pi/4$							/
$\pi/2$						/	
$3\pi/4$				/			

Finding the possible lines and updating the histogram matrix for the remaining 6 points, we obtain:

	-3	-2	-1	0	1	2	3
0		//			/	////	
$\pi/4$	/			///	/	/	/
$\pi/2$		//	//		/	//	
$3\pi/4$	/	/	//	//			/

Identifying the two lines with the maximum number of hits:

Line 1: $[\mathbf{r}_1, \mathbf{q}_1] = [2, 0]$ Line 2: $[\mathbf{r}_2, \mathbf{q}_2] = [0, \pi/4]$

Examining the detected lines on the image with the strong edge points, we obtain agreeable results:

